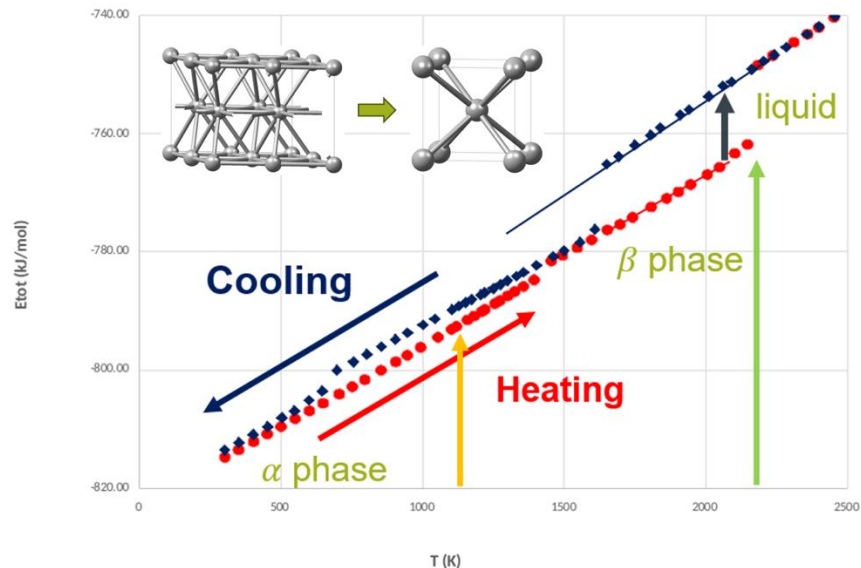


# Precision at Scale with Machine-Learned Potentials

Volker Eyert and Jörg-Rüdiger Hill

December 10-12, 2025



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# GoTo Webinar Interface – Please Ask Questions!

The screenshot displays the GoTo Webinar interface. At the top, it shows "Main room" and a timer at "46:14". A status bar at the top center indicates "No active cameras". A red circle highlights the chat icon in the top right corner. A white box with a black border points to the chat icon with the text "Access chat interface." Below the main content area, a toolbar contains icons for chat, document, settings, and a menu. A "Chat" window is open, showing a message from the organizer at "01:01 AM" that says "This is a message to everyone." A white box with a black border points to the chat window with the text "Use the chat interface to ask questions." The main content area shows a microphone icon and the text "Nobody has turned on their camera yet". At the bottom, there are controls for Record, React, Mic, Camera, Share, Leave, and Captions.



# Webinar Speakers

*Katherine Hollingsworth*

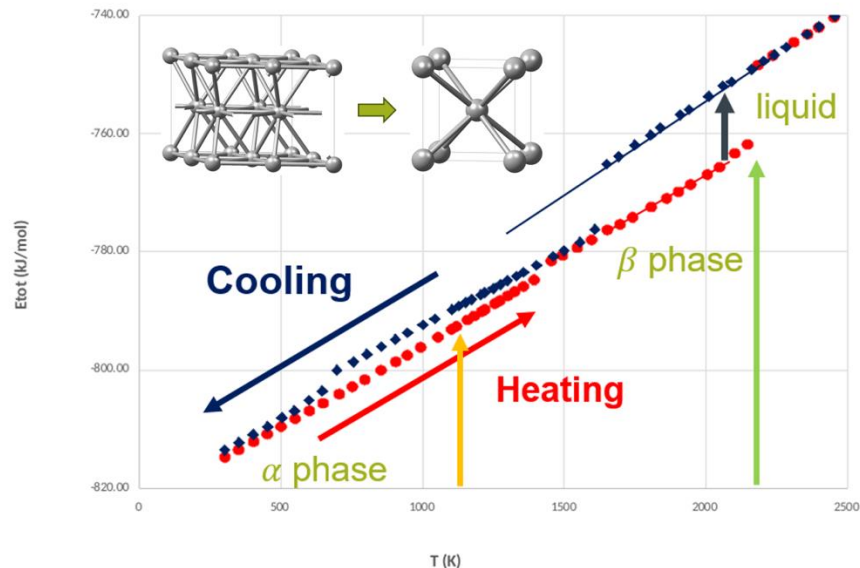
*Dr. Volker Eyert*

*Dr. Jörg-Rüdiger Hill*

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# Corrosion

The global cost of corrosion is estimated to be US\$2.5 trillion, which is equivalent to 3.4% of the global GDP. Numerous industries are affected including:

## 1) Energy:

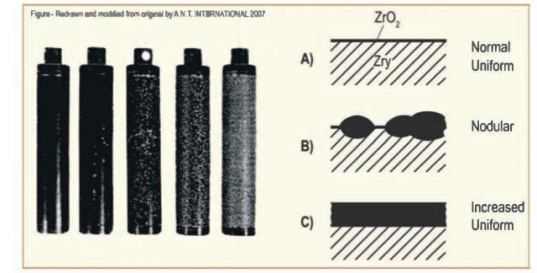
- Water-cooled reactors
  - Corrosion of fuel cells is one of the major life-limiting degradation mechanism in these reactors

## 2) Energy:

- Oil & Gas
  - Corroding pipelines and various equipment in Oil and gas

## 3) Automotive:

- Magnesium alloys have been used due to their mechanical properties and castability but they have poor corrosion resistance.



R. Adamson et al., *Corrosion mechanisms in zirconium alloys, ZIRAT12 Special Topic Report* (2007)

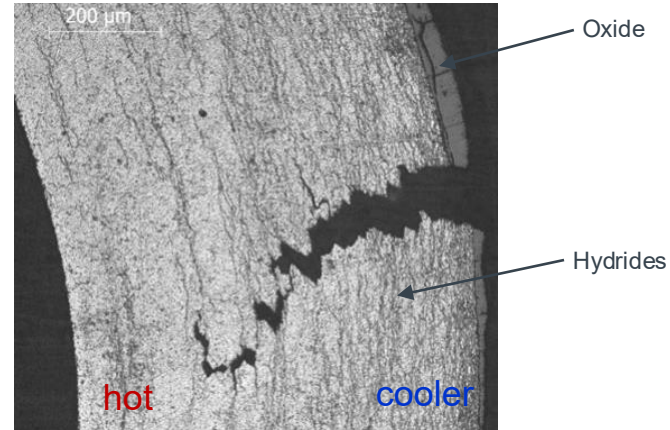


M. Askari, M. Aliofkhaezaei, and S. Afroukhteh, *J. Nat. Gas Sci. Eng.* **71**, 102971 (2019) <https://doi.org/10.1016/J.JNGSE.2019.102971>

# Hydrogen Embrittlement of Zirconium Alloys

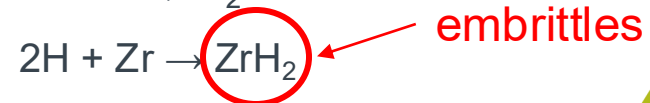


95% Zr; Sn, Nb, Fe, O can be present

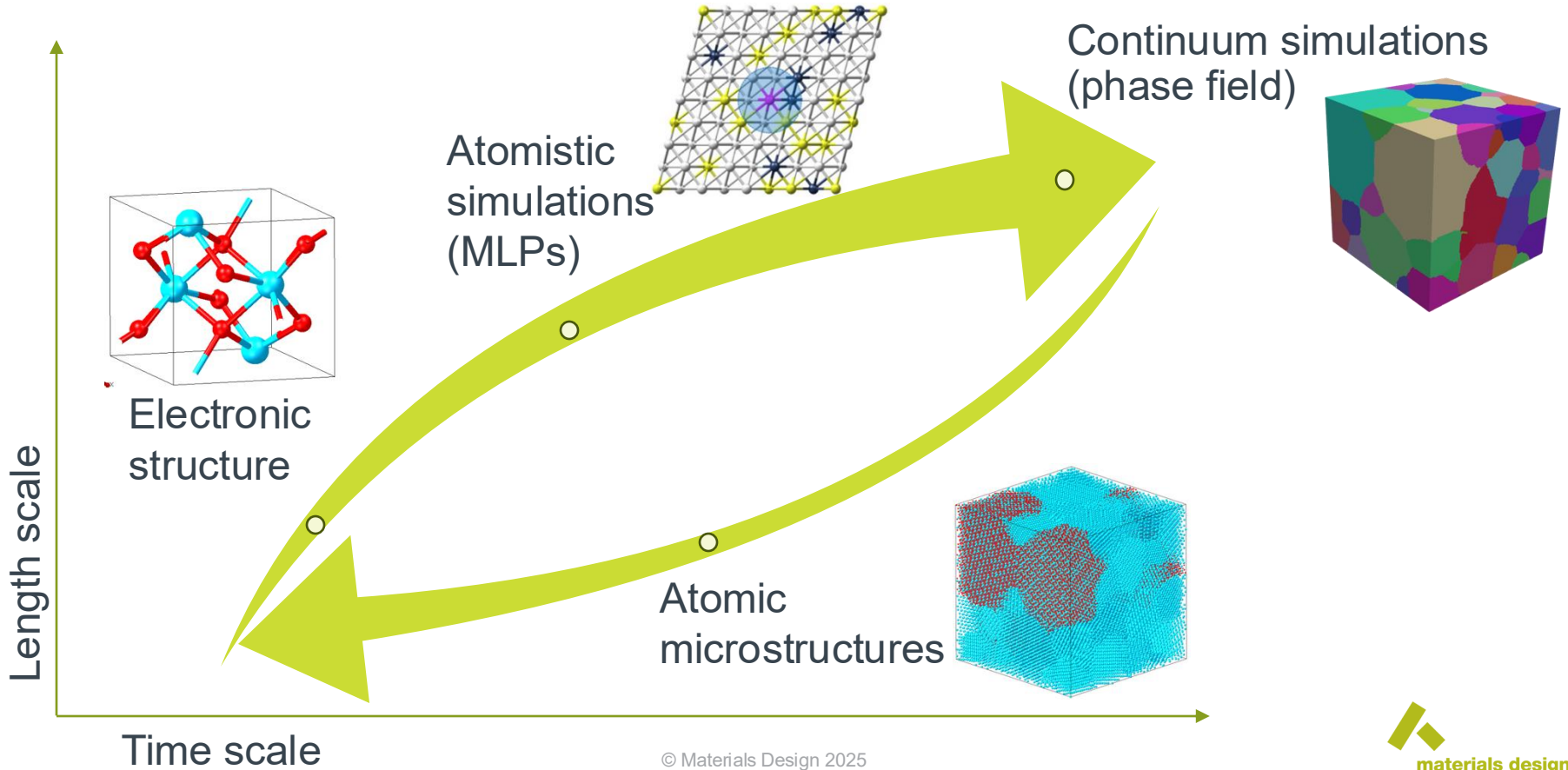


Cross section of fuel rod, Zr alloy

Corrosion of Zr alloys:



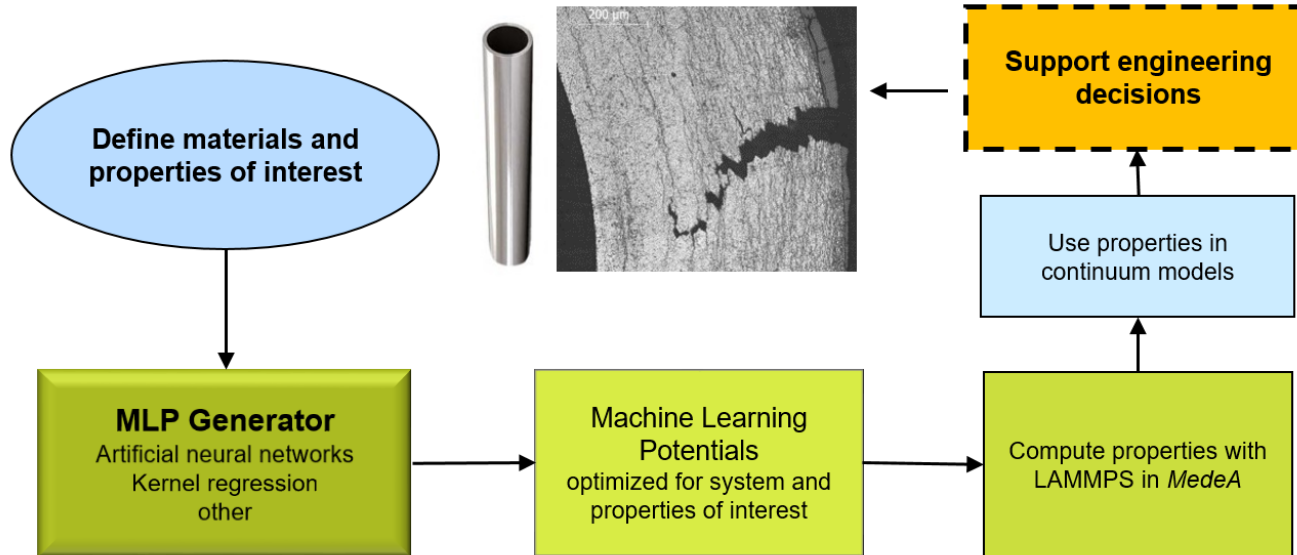
# Bridging time and length scales



# Back in 2020

## The vision

- Creation of an **A**dvanced **M**aterials **S**imulation **E**ngineering **T**ool for reliable large-scale simulations of thermomechanical and chemical properties of engineering materials



# Back in 1998

4596

*J. Phys. Chem. A* **1998**, *102*, 4596–4605

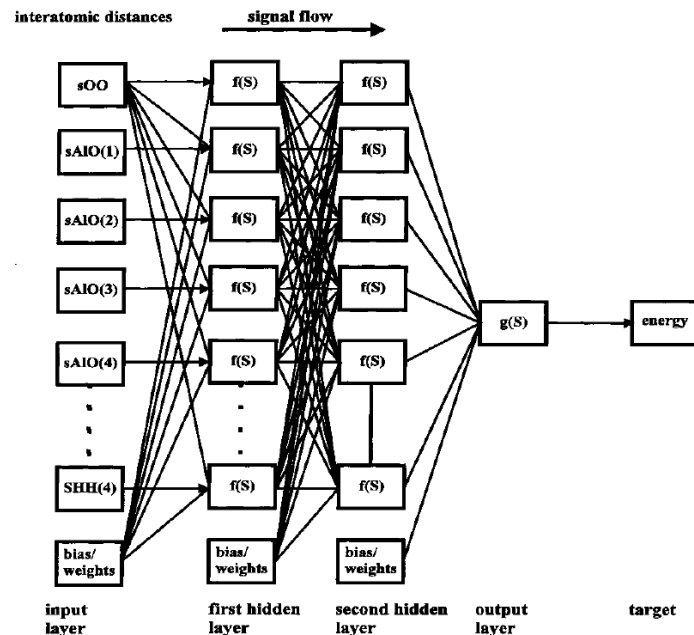
## Representation of Intermolecular Potential Functions by Neural Networks

Helmut Gassner,<sup>†</sup> Michael Probst,<sup>\*,†</sup> Albert Lauenstein,<sup>‡</sup> and Kersti Hermansson<sup>‡</sup>

*Institute of General and Inorganic Chemistry, Innsbruck University, Innrain 52a, A-6020 Innsbruck, Austria, and Inorganic Chemistry, The Ångström Laboratory, Uppsala University, Box 538, S-75121 Uppsala, Sweden*

*Received: July 8, 1997; In Final Form: March 17, 1998*

We have investigated how a neural network representation of intermolecular potential functions can be used to elevate some of the problems commonly encountered during fitting and application of analytical potential functions in computer simulations. For this purpose we applied feed-forward networks of various sizes to reproduce the three-body interaction energies in the system  $\text{H}_2\text{O}-\text{Al}^{3+}-\text{H}_2\text{O}$ . In this highly polarizable system the three-body interaction terms are necessary for an accurate description of the system, and it proved difficult to fit an analytical function to them. Subsequently we performed Monte Carlo simulations on an  $\text{Al}^{3+}$  ion dissolved in water and compared the results obtained using the neural network type potential function with those using a conventional analytical potential. The performance and results of our calculations lead to the conclusion that, for suitable systems, the advantages of a neural network type representation of potential functions as a model-independent and “semiautomatic” potential function outweigh the disadvantages in computing speed and lack of interpretability.



**Figure 1.** Architecture of the feed-forward network. The input consists of a vector of interatomic distances which are processed to calculate the energy.

# The 2000s and 2010s

- S. Manzhos and T. Carrington, *A random-sampling high dimensional model representation neural network for building potential energy surfaces*, J. Chem. Phys. **125**, 084109 (2006).
- J. Behler and M. Parrinello, *Generalized Neural-Network Representation of High-Dimensional Potential-Energy Surfaces*, Phys. Rev. Lett. **98**, 146401 (2007).
- A. P. Bartók, M. C. Payne, R. Kondor, and G. Csányi, *Gaussian Approximation Potentials: The Accuracy of Quantum Mechanics, without the Electrons*, Phys. Rev. Lett. **104**, 136403 (2010).
- A. P. Thompson, L. P. Swiler, C. R. Trott, S. M. Foiles, and G. J. Tucker, *Spectral neighbor analysis method for automated generation of quantum-accurate interatomic potentials*, J. Comp. Phys. **285**, 316 (2015).
- A. V. Shapeev, *Moment Tensor Potentials: A Class of Systematically Improvable Interatomic Potentials*, Multiscale Model. Simul. **14**, 1153 (2016).
- R. Drautz, *Atomic cluster expansion for accurate and transferable interatomic potentials*, Phys. Rev. B **99**, 014104 (2019); Phys. Rev. B **100**, 249901(E) (2019).

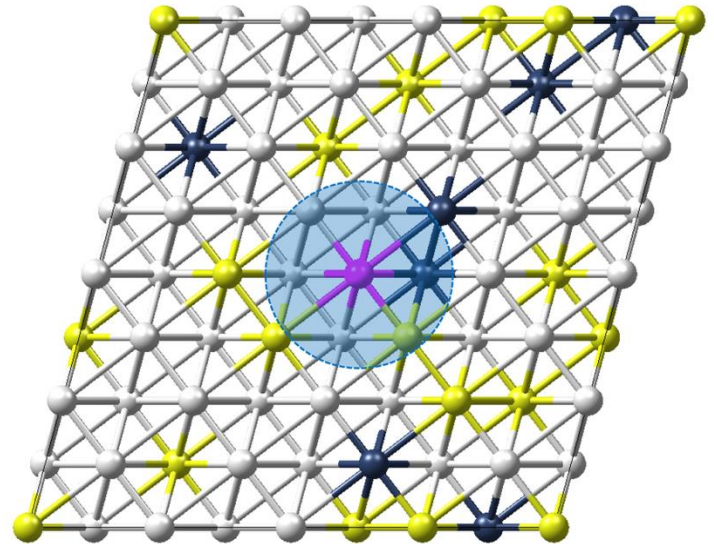
# Agenda

- Motivation
- MLP Product Line
- Selected Applications
  - Equilibrium properties
  - Phase transitions
  - Nanoparticles
  - Surface Interactions
  - Zeolites
- Concluding Remarks

# Acknowledgements

- All colleagues at Materials Design, especially
  - David Reith, Leonid Kahle, Mikael Christensen, Marthe Bideault, Garrett Tow, Shubham Pandey, Michele Kotiuga, Clint Geller, Marianna Yiannourakou, and Erich Wimmer
- Customers of Materials Design, especially
  - Jonathan Wormald (Naval Nuclear Laboratory)
  - The machine-learned potential (MLP) work was funded by the Advanced Materials Simulation Engineering Tool (AMSET) project sponsored by NNL
- Science and technology partners, especially
  - Ralf Drautz, Matous Mrovec, Yury Lysogorskiy, Anton Bochkarev, Minaam Qamar

# MLPs in *MedeA*



# MedeA MLP Generator

Collection of tools to generate MLPs from user-created training sets for subsequent use with *MedeA* LAMMPS

## Spectral Neighbor Analysis Potential (**SNAP**/q**SNAP**)

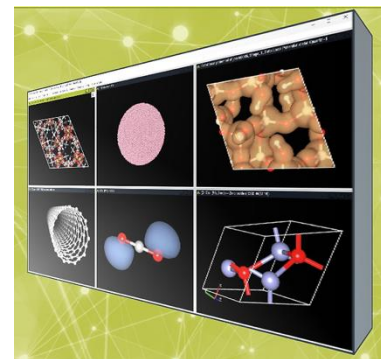
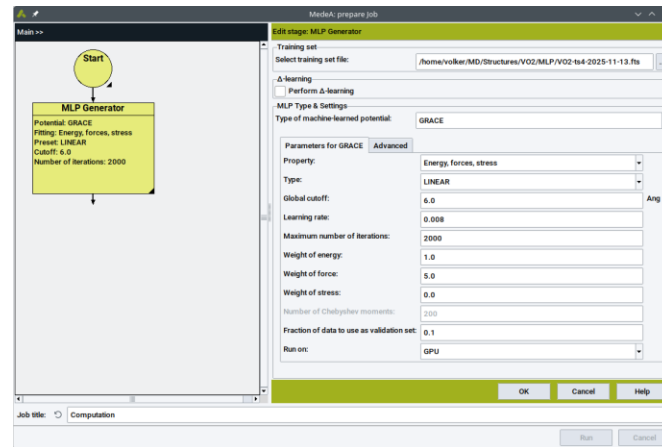
- A. Thompson and M. Wood
- FitSNAP code by Sandia group

## Neural Network Potential (**NNP**)

- J. Behler and M. Parrinello
- n2p2 code by A. Singraber, Vienna

## Atomic Cluster Expansion (**ACE**) and Graph ACE (**GRACE**)

- R. Drautz, Y. Lysoy, A. Bochkarev, and M. Mrovec
- PACEMAKER/GRACEMAKER code by ICAMS group





# MedeA MLPs

## Collection of pre-trained MLPs ready to use with MedeA LAMMPS

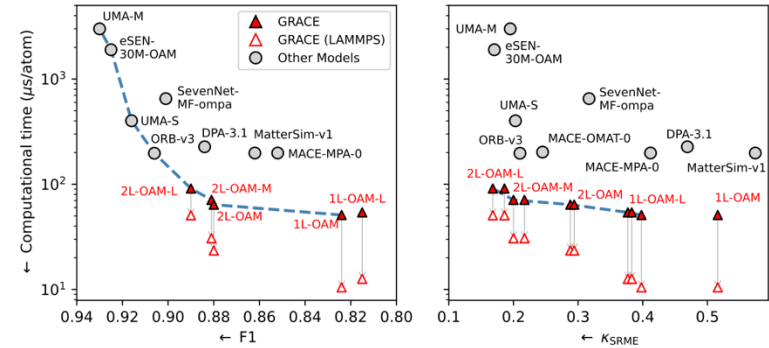


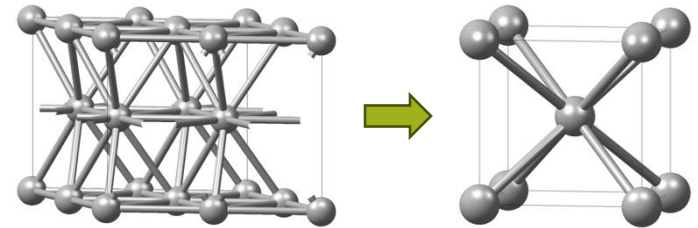
FIG. 1. Model performance for stable structure identification (F1 score in MatBench Discovery benchmark) and thermal conductivity prediction ( $\kappa_{SRME}$ ) versus computational time per atom. A higher F1 score and lower  $\kappa_{SRME}$  indicate better performance. The blue dashed line links Pareto optimal models. Computational performance is estimated via ASE (filled symbols) and LAMMPS (open symbols), with GRACE models indicated in red.

## Foundational GRACE

- **Validated Accuracy:** Top-ranking in most recent MatBench competitions.
- **Complex property prediction:** Accurately predicts challenging properties, such as thermal conductivity and elastic moduli.
- **Unmatched Efficiency:** Establishes a new '**Pareto front**', offering the best available balance between **high accuracy** and **computational speed**.

# Zirconium

Phase Transitions, Defects, Elastic and Vibrational Properties



# Training Set Creation

Retrieve initial structures from *MedeA* InfoMaticA, the internal structure database



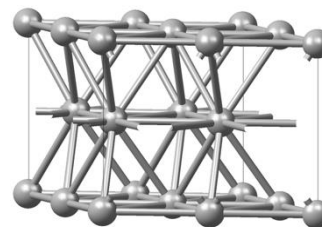
Build strained cells, create randomly perturbed and substituted structures, and perform single-point calculations



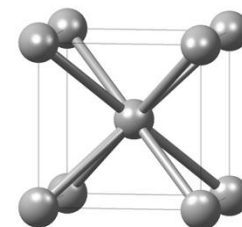
Build supercells w/wo self-interstitial atoms and vacancies, surfaces, stacking faults and perform NPT/NVT MD MLFF simulations at 300-1700 K



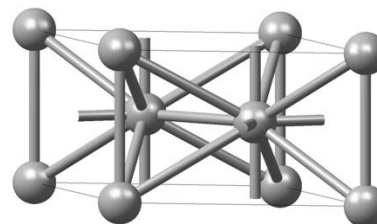
Training set structures



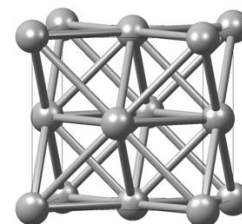
$\alpha$ -phase, hcp



$\beta$ -phase, bcc



$\omega$ -phase, hex

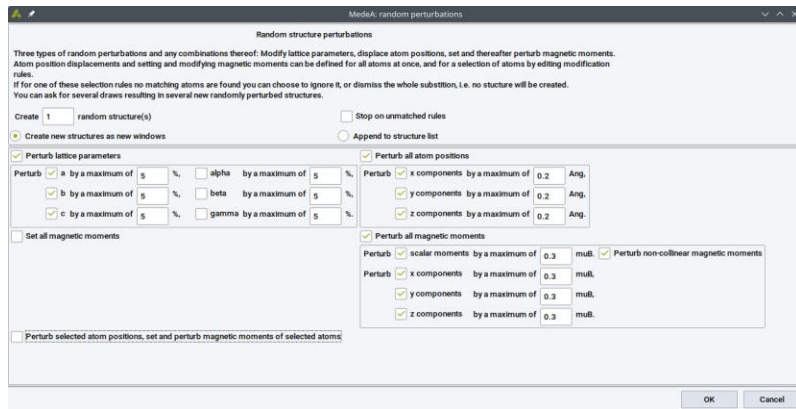


fcc

All calculations use  
*MedeA* High-Throughput

# Training Set Creation

Retrieve initial structures from *MedeA* InfoMaticA, the internal structure database



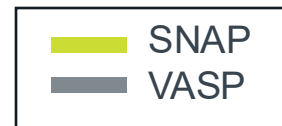
Training set structures

## *MedeA* Random Perturbation/Substitution tools

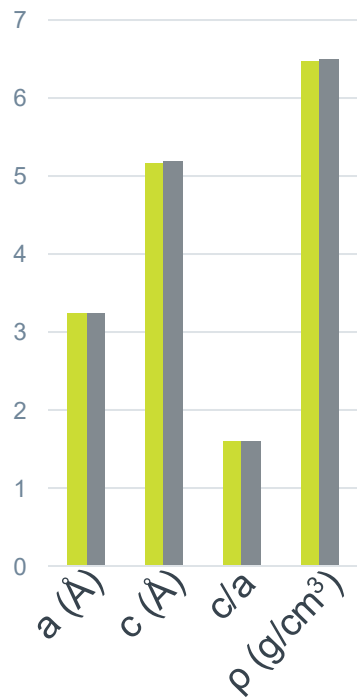
- Introduce random perturbations of lattice vectors, atomic positions, magnetic moments
- Introduce random changes of atomic species
- Create an arbitrary number of structures
- Results can be appended to structure lists for subsequent high-throughput calculations

All calculations use  
*MedeA* High-Throughput

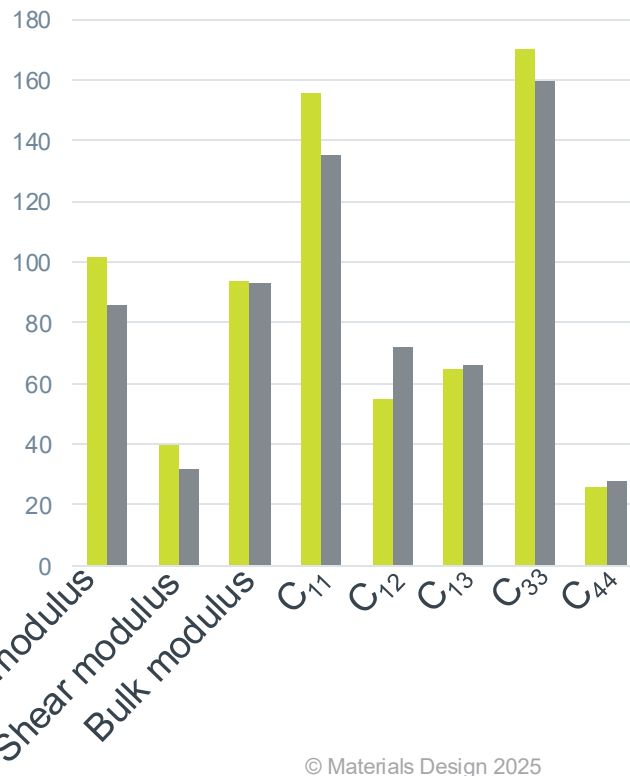
# $\alpha$ -Zr: MLP agreement with VASP training data



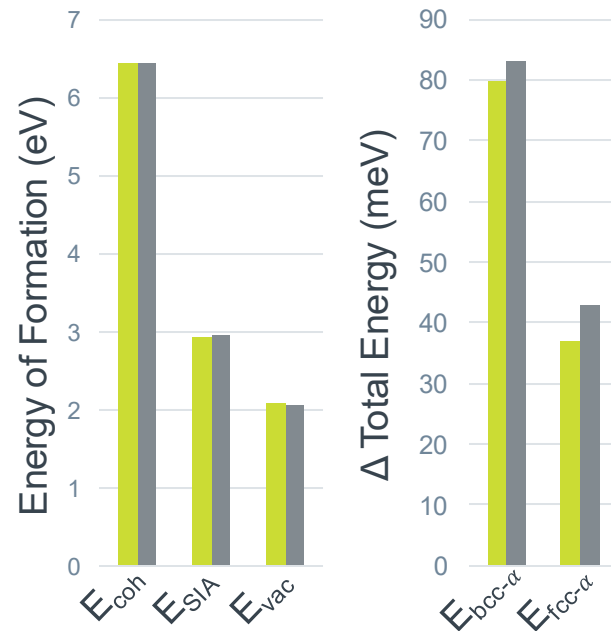
## Structural properties



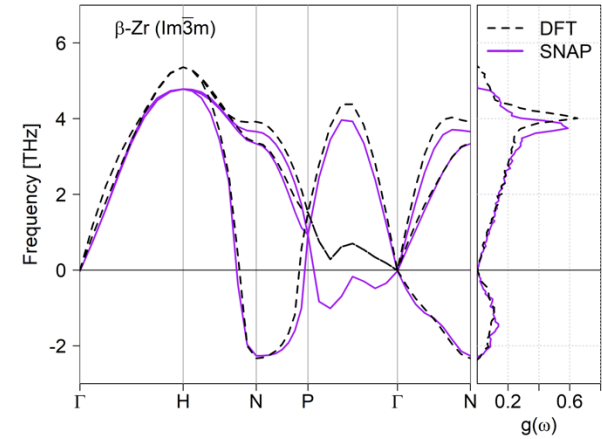
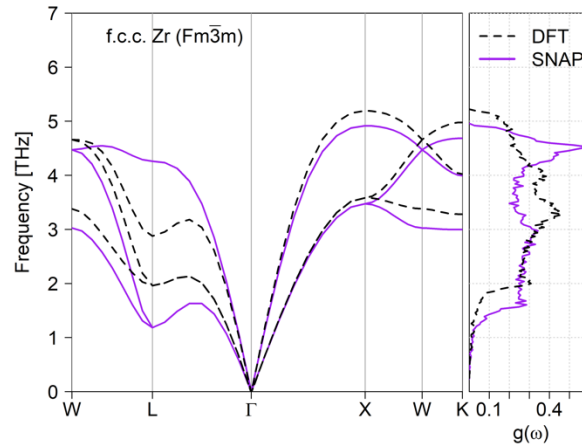
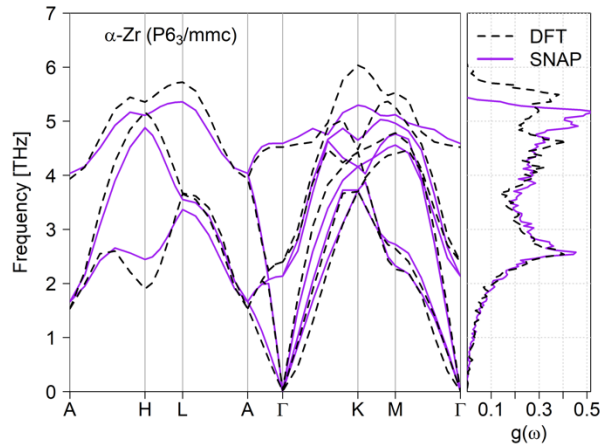
## Elastic properties (GPa)



## Energetics

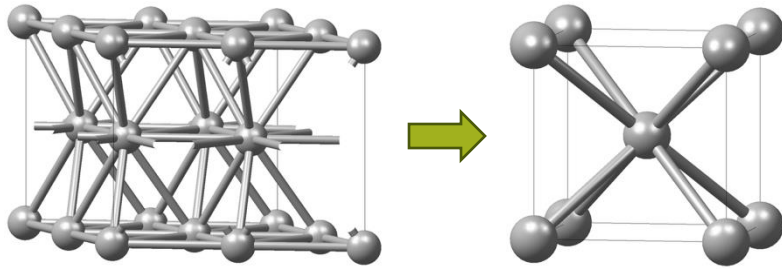


# $\alpha$ -Zr: SNAP Agreement with VASP Training Data



N-point phonon instability  
is a precursor of the bcc  
→ hcp phase transition

# Zr: $\alpha$ - $\beta$ Phase Transition

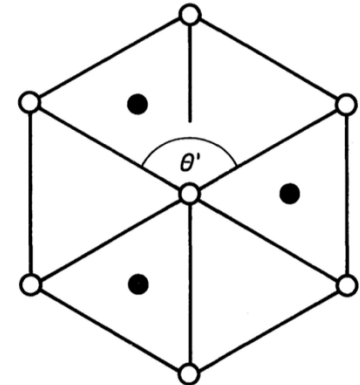
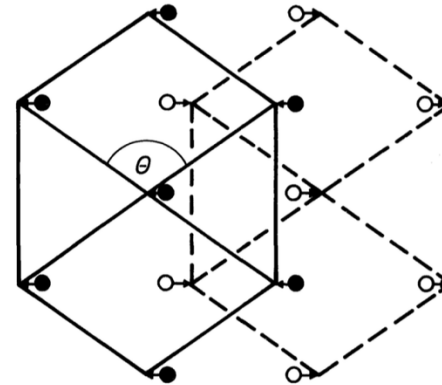
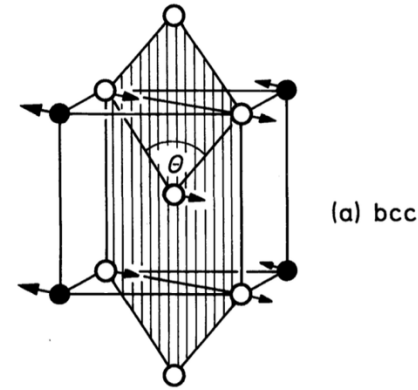


Martensitic phase transition at  $\approx 1135$  K

- high-T bcc  $\rightarrow$  low-T hcp
- collective motion of atoms
- instability of bcc N-point  $T_1$  phonon

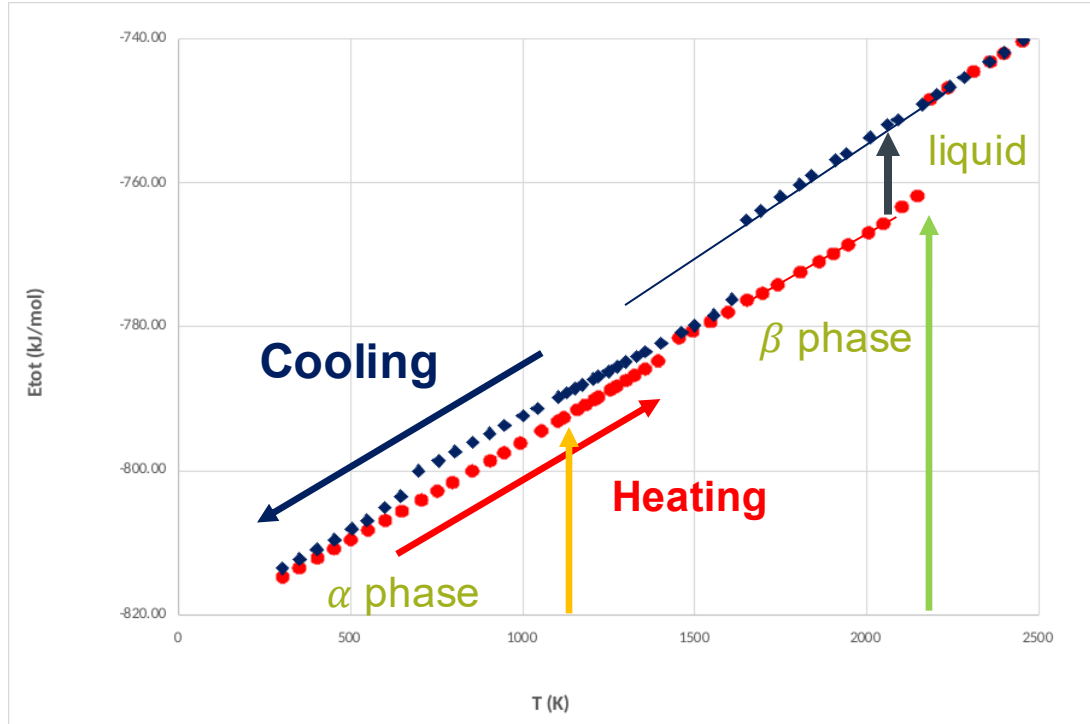
Structural changes

- involve (110) planes of bcc structure
- relative shift of neighboring (110) planes
- change of in-plane angle from  $\Theta = 109.47^\circ$  to  $\Theta' = 120^\circ$



J. Kübler and V. Eyert, *Electronic structure calculations*, in: *Electronic and Magnetic Properties of Metals and Ceramics*, ed. K. H. J. Buschow (VCH Verlagsgesellschaft, Weinheim 1992), pp. 1-145

# Zr: $\alpha$ - $\beta$ Phase Transition



Transition temperatures (exp):

- $\alpha$ - $\beta$  transition: 1135 K
- melting: 2128 K

Latent heat of  $\alpha$ - $\beta$  transition:

- MLP:  $\Delta H = 2.5$  kJ/mol
- Exp.:  $\Delta H = 4.0$  kJ/mol

Heat of fusion:

- MLP:  $\Delta H = 13$  kJ/mol
- Exp.:  $\Delta H = 14$ -17 kJ/mol

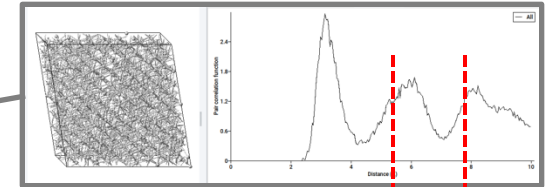
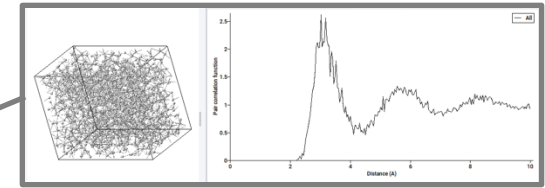
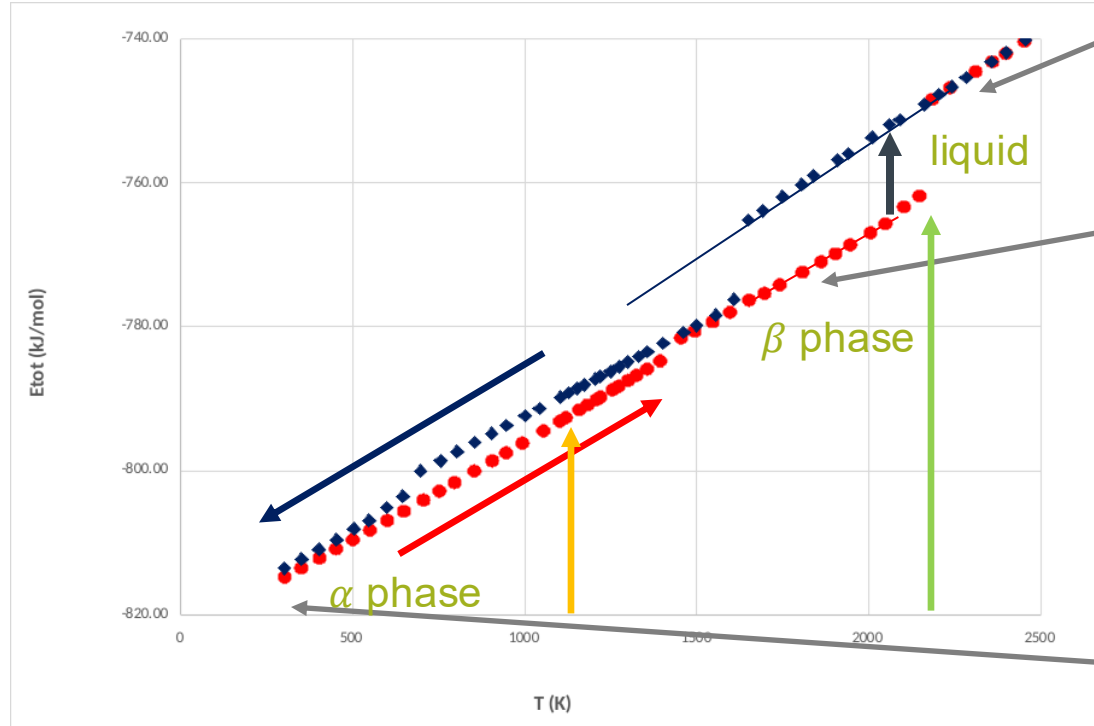
Specific heat:

- MLP:  $c_p = 25$ -31 J/(mol·K)
- Exp.:  $c_p = 25$ -39 J/(mol·K)

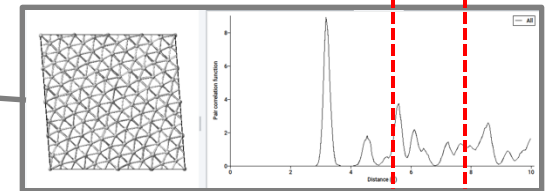
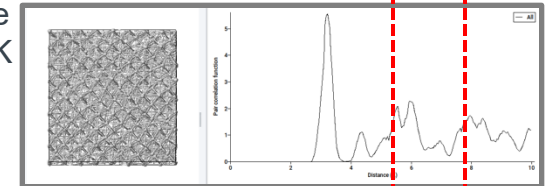
E. S. Fisher and C. J. Renken, Phys. Rev. **135**, A482 (1964);  
M. W. Chase, jr., J. Phys. Chem. Ref. Data **9**, 1 (1998).

**MLP capable of capturing multiple coordination environments!**

# Zr: $\alpha$ - $\beta$ Phase Transition

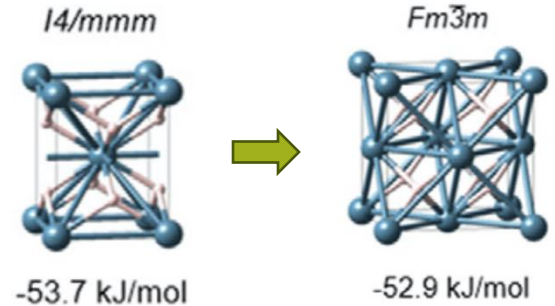


$\beta$  phase  
at 300 K



# Zirconium Hydrides

Phase Transitions and Elastic and Vibrational Properties



# Training Set for ZrH<sub>x</sub>

J. Phys.: Condens. Matter 27 (2015) 025402

M Christensen *et al*

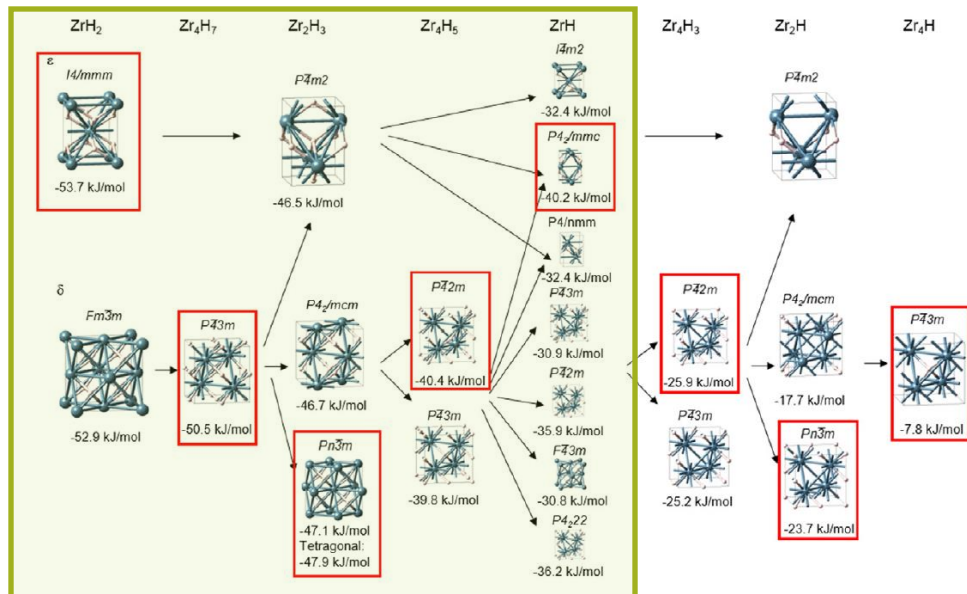


Figure 4. Hydride structures based on ABC stacking of Zr atoms. The most stable structure for each stoichiometry is circled.



# ZrH<sub>x</sub>: Lattice Parameters

## $\gamma$ -ZrH (P4<sub>2</sub>/mmc)

|       | Weck | PBE  | BMD19.3 | SNAP | NNP  |
|-------|------|------|---------|------|------|
| a (Å) | 4.59 | 4.59 | 4.89    | 4.58 | 4.58 |
| c (Å) | 5.02 | 4.99 | 4.49    | 5.00 | 5.01 |

face-centered  
tetragonal setting

## $\epsilon$ -ZrH<sub>2</sub> (I4/mmm)

|       | Weck | PBE  | BMD19.3 | SNAP | NNP  |
|-------|------|------|---------|------|------|
| a (Å) | 5.02 | 4.99 | 4.85    | 5.00 | 5.08 |
| c (Å) | 4.42 | 4.42 | 4.85    | 4.42 | 4.24 |

face-centered  
tetragonal setting

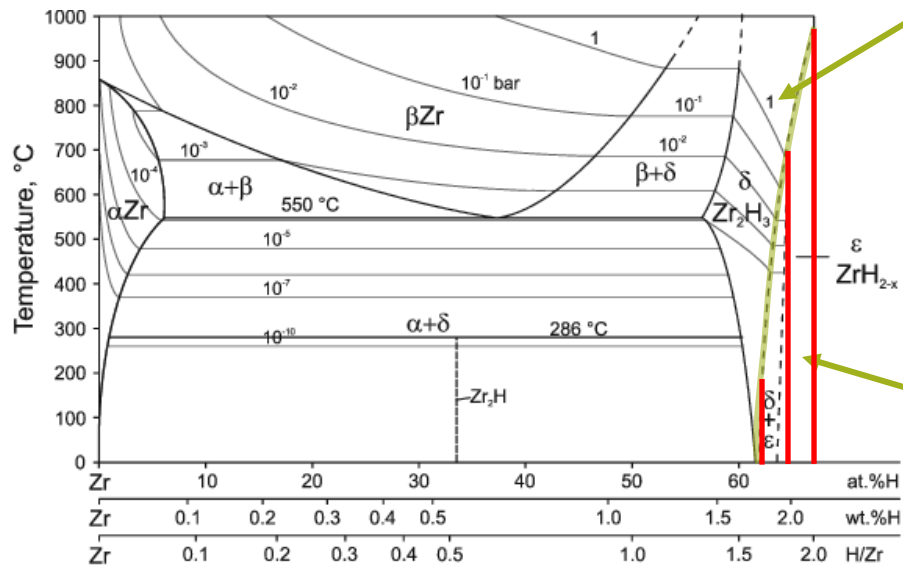
Weck *et al.*, Dalton Trans. **44**, 18769 (2015): VASP PBE

# ZrH<sub>x</sub>: Elastic Coefficients and Moduli

$\epsilon$ -ZrH<sub>2</sub> (I4/mmm)

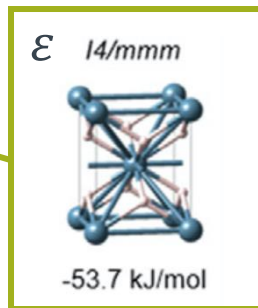
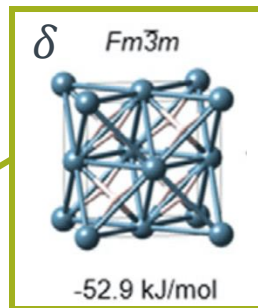
|                 | GPa | Weck | Zhang | PBE | BMD19.3 | SNAP | NNP |
|-----------------|-----|------|-------|-----|---------|------|-----|
| C <sub>11</sub> | 180 | 164  | 176   | 246 | 169     | 217  |     |
| C <sub>12</sub> | 151 | 147  | 146   | 161 | 153     | 175  |     |
| C <sub>13</sub> | 115 | 110  | 104   | 161 | 103     | 129  |     |
| C <sub>33</sub> | 152 | 146  | 159   | 246 | 151     | 159  |     |
| C <sub>44</sub> | 23  | 30   | 62    | 84  | 35      | 65   |     |
| C <sub>66</sub> | 65  | 61   | 82    | 84  | 51      | 64   |     |
| B               | 139 | 132  | 134   | 189 | 132     | 156  |     |
| S               | 28  | 26   | 44    | 64  | 27      | 44   |     |
| Y               | 77  | 73   | 118   | 172 | 76      | 121  |     |

# $\epsilon$ - $\delta$ -Transition of $ZrH_x$

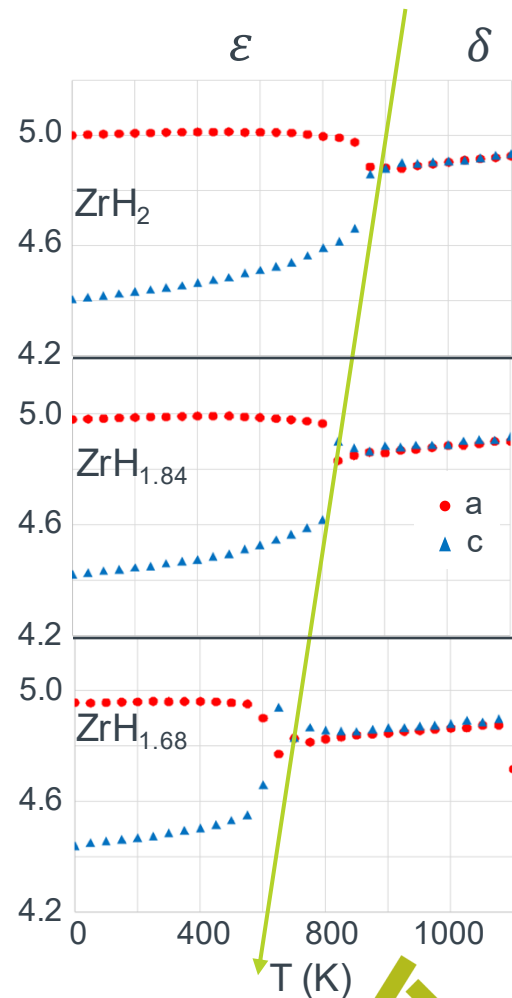


Grosse et al., Oxid Met **70**, 149 (2008)

Sharp decrease of transition temperature with increasing number of H vacancies.

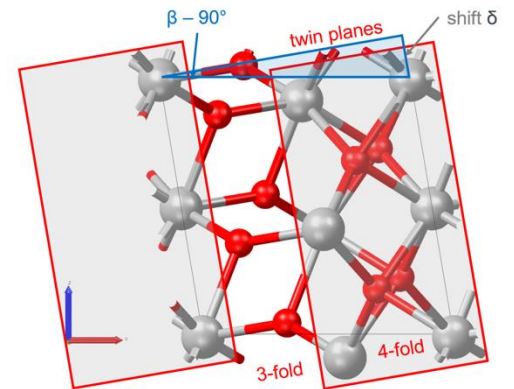


Lattice Parameter (Å)



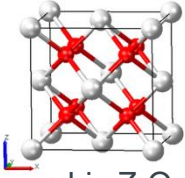
# Zirconium Oxides

Phase Transitions, Defect, and Microstructures



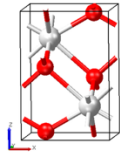
# Phase Transitions of ZrO<sub>2</sub>

$\rho = 6.141 \text{ g/cm}^3$



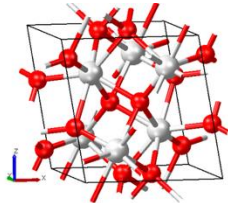
cubic ZrO<sub>2</sub>

$\rho = 6.099 \text{ g/cm}^3$

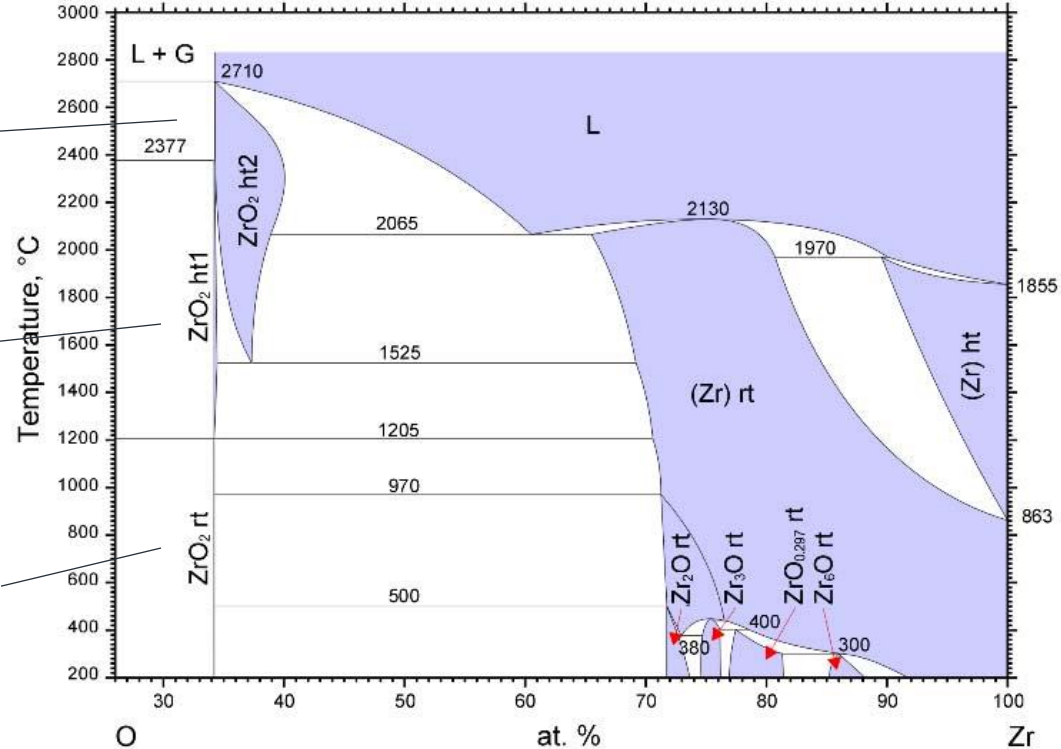


tetragonal ZrO<sub>2</sub>

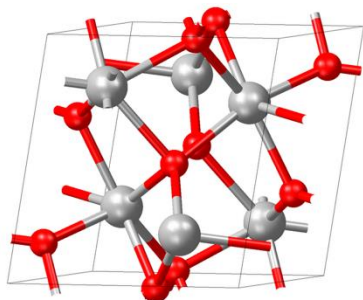
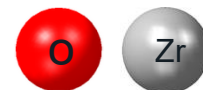
$\rho = 5.819 \text{ g/cm}^3$



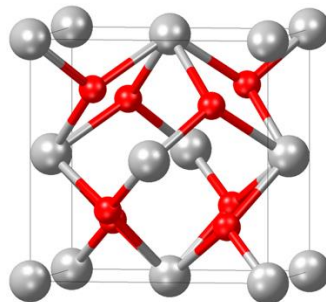
monoclinic ZrO<sub>2</sub>



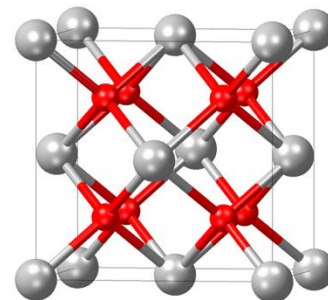
# Training Set for $\text{ZrO}_x$



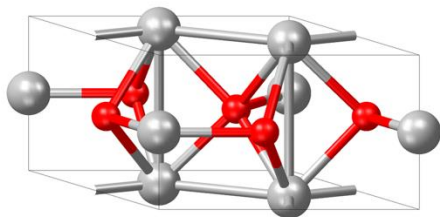
$\text{ZrO}_2$  mon



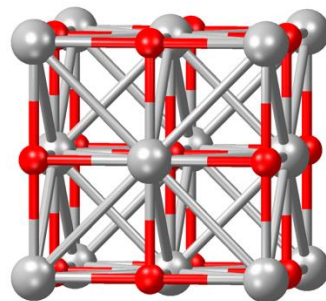
$\text{ZrO}_2$  tet



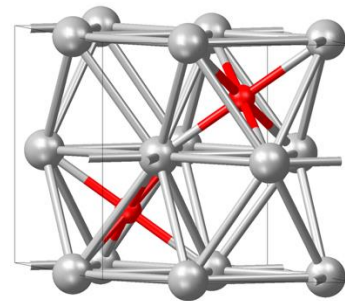
$\text{ZrO}_2$  fcc



ZrO hex

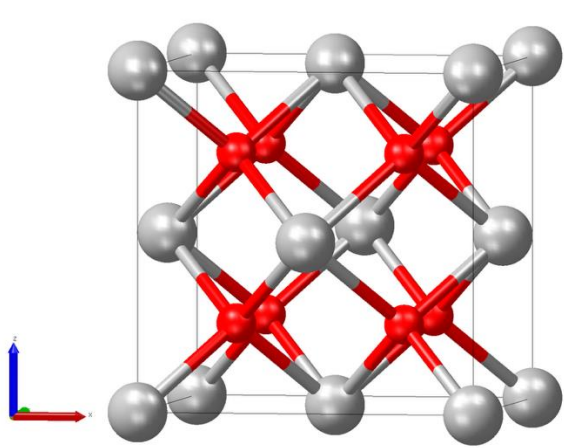


ZrO fcc

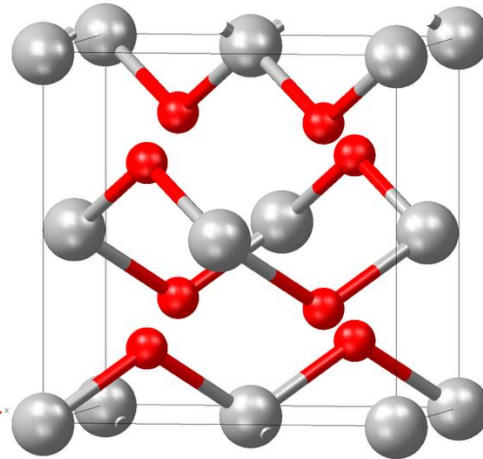


$\text{Zr}_3\text{O}$  hex

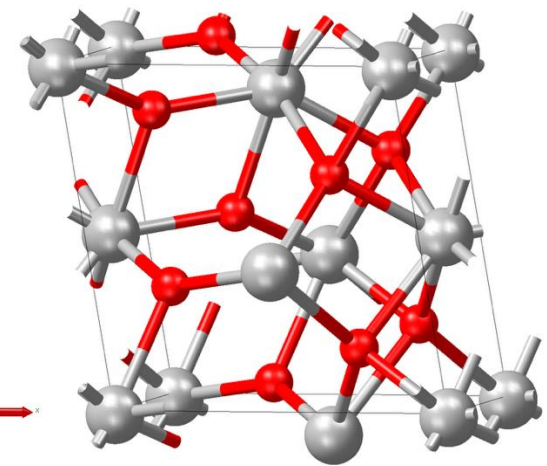
# Phase Transitions of $\text{ZrO}_2$



cubic



tetragonal



monoclinic

Displacive phase transition at  $\approx 2580$  K

- high-T cubic  $\rightarrow$  low-T tetragonal
- instability of fcc X-point phonon

Structural changes

a) Disproportionation of Zr-O bond lengths

Martensitic phase transition at  $\approx 1400$  K

- high-T tetragonal  $\rightarrow$  low-T monoclinic

Structural changes

a) Formation of twin Zr planes

b) O coordination: 4-fold  $\rightarrow$  3-fold

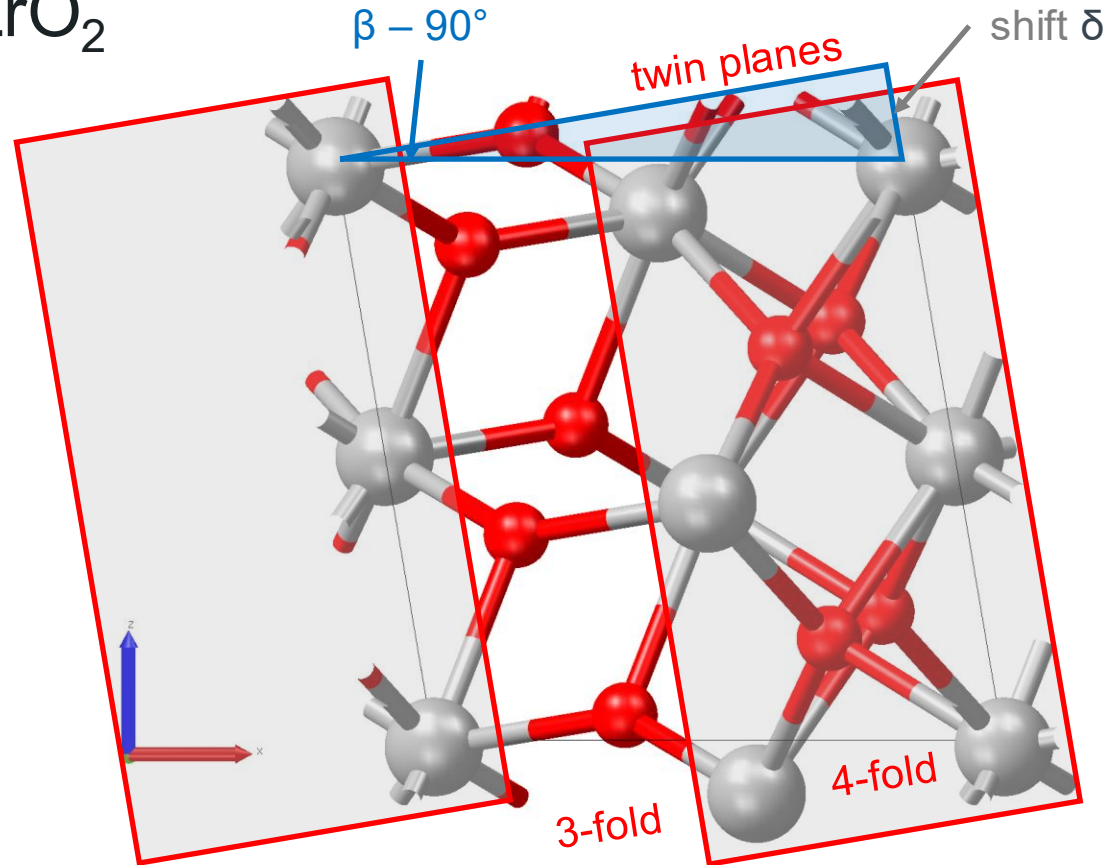
# Phase Transitions of $\text{ZrO}_2$

Martensitic phase transition

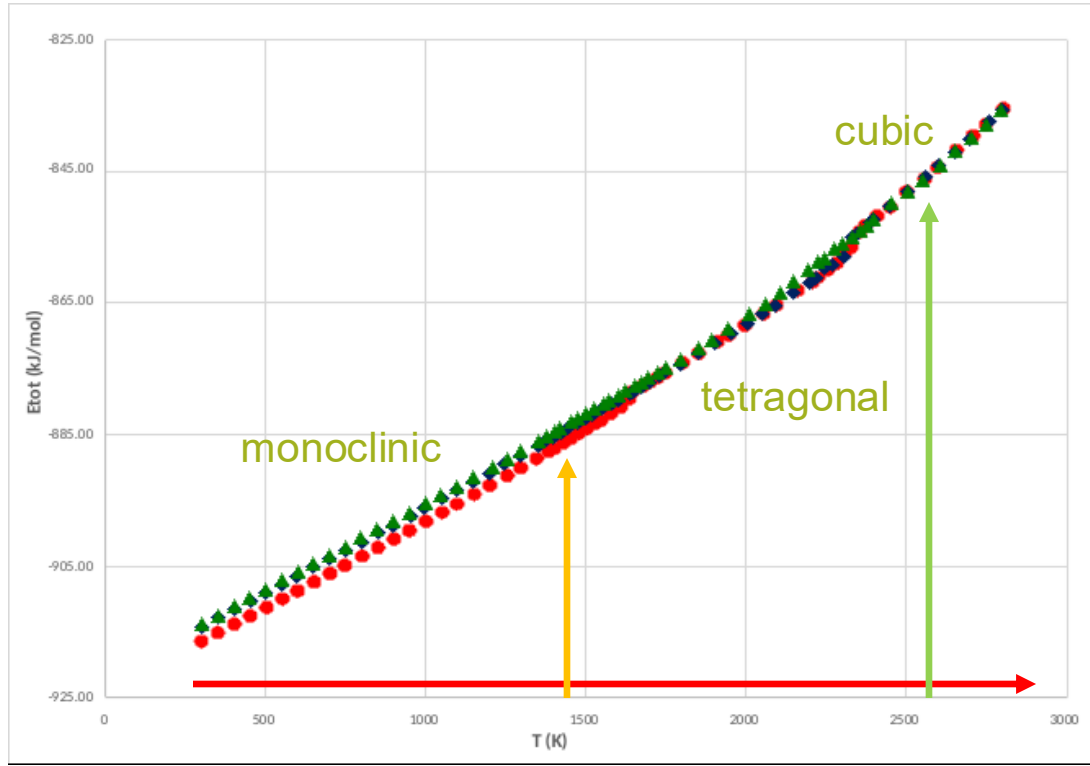
- high-T tetragonal  $\rightarrow$  low-T monoclinic

Structural changes

- a) formation of twin Zr planes
- b) lateral shift  $\delta$  of neighboring twin planes  $\rightarrow$  induces monoclinic angle  $\beta \neq 90^\circ$  with  $\delta = a_{\text{lat}} \times \sin(\beta - 90^\circ)$
- c) 4-fold O coordination within twin planes
- d) 3-fold O coordination across twin planes

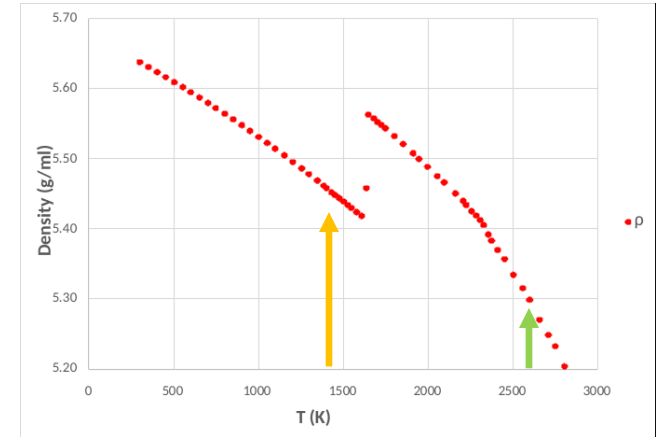


# Phase Transitions of ZrO<sub>2</sub>



Transition temperatures (exp):

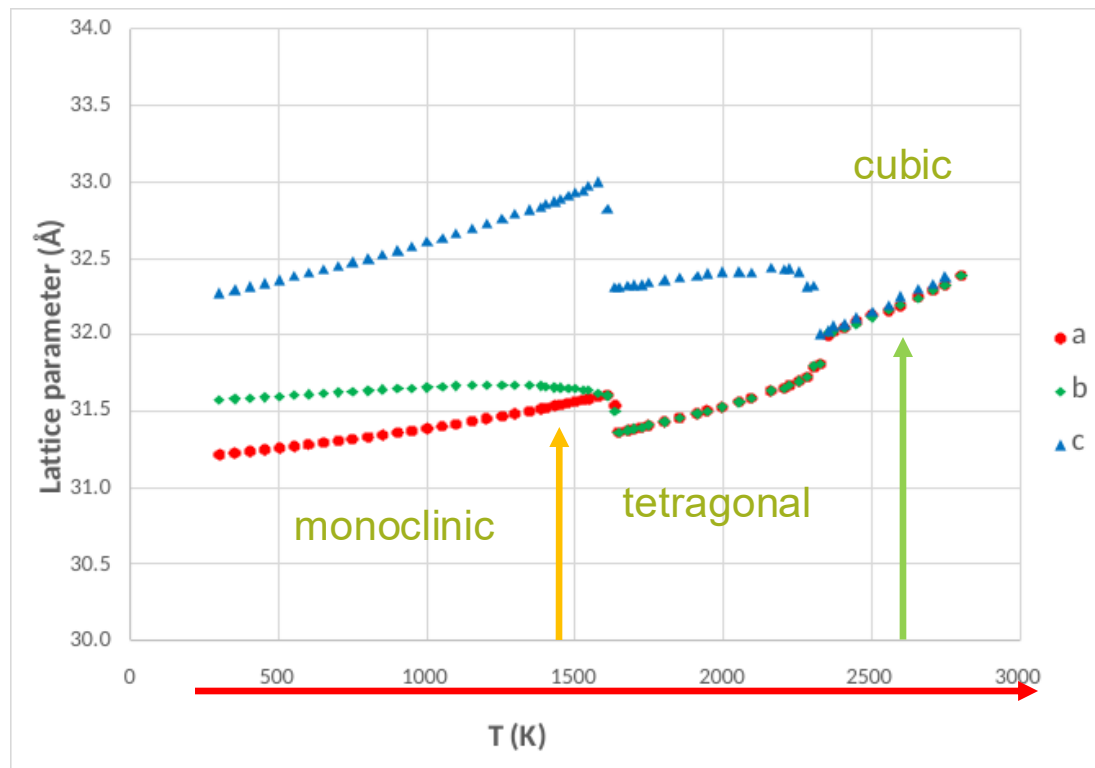
- **mon-tet transition:**
  - 1430-1474 K (heating)
  - 1305-1264 K (cooling)
- **tet-cub:** 2584 K



A. Navrotsky et al., J. Am. Ceram. Soc. **88**, 2942 (2005);  
C. Wang et al., J. Am. Ceram. Soc. **89**, 3751 (2006);  
M. Mamivand et al., Acta Mater. **61**, 5223 (2013)

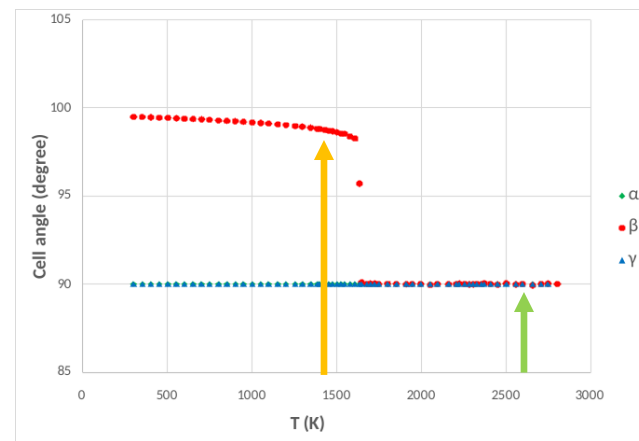
**MLP capable of capturing multiple coordination environments!**

# Phase Transitions of ZrO<sub>2</sub>



Transition temperatures (exp):

- **mon-tet transition:**
  - 1430-1474 K (heating)
  - 1305-1264 K (cooling)
- **tet-cub:** 2584 K



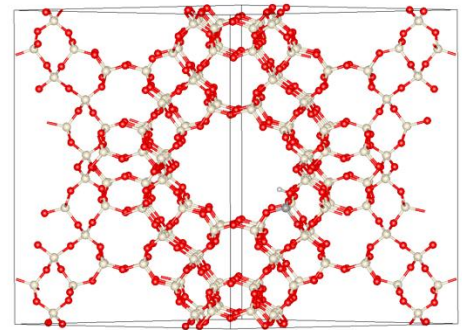
A. Navrotsky et al., J. Am. Ceram. Soc. **88**, 2942 (2005);  
C. Wang et al., J. Am. Ceram. Soc. **89**, 3751 (2006);  
M. Mamivand et al., Acta Mater. **61**, 5223 (2013)

**MLP capable of capturing multiple coordination environments!**

# Phase Transition

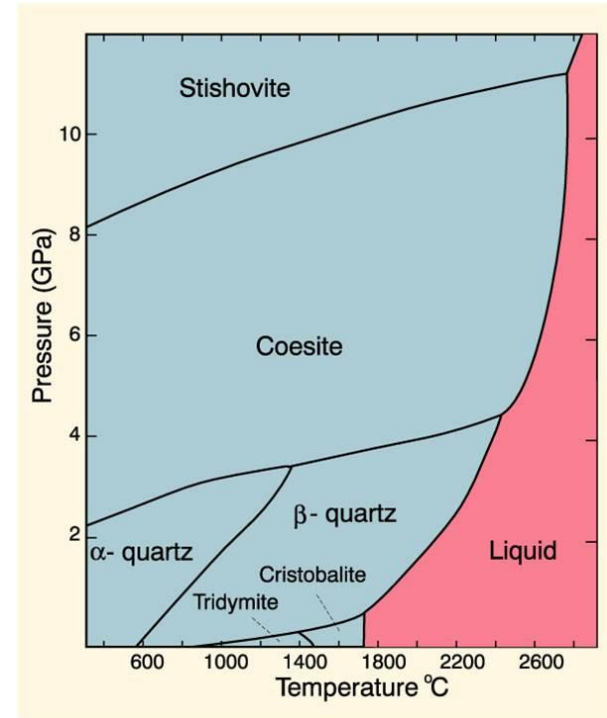
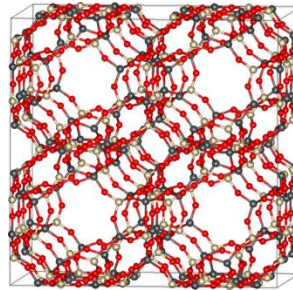
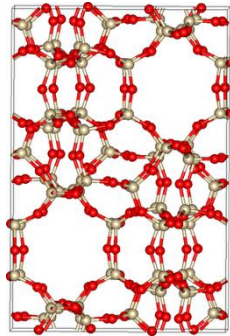
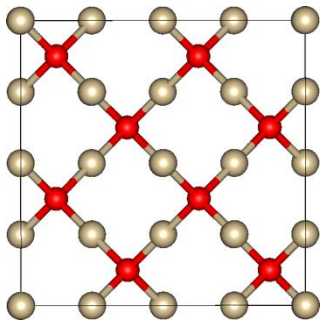
**Heating of m-ZrO<sub>2</sub>**  
**Stoichiometric and with 5% O-Vacancies**

# SiO<sub>2</sub> Polymorphs and Zeolites



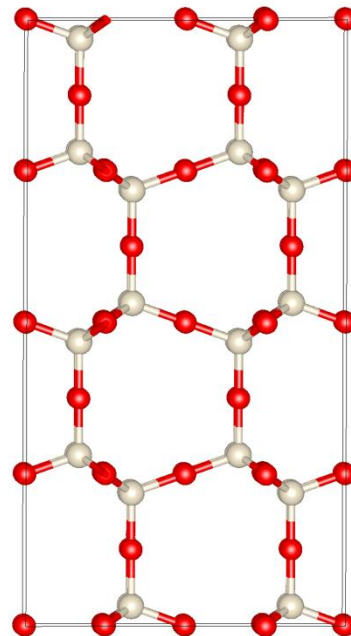
# SiO<sub>2</sub> polymorphs and zeolites

- Covalently bonded oxide structures
- Structurally very diverse
- Densely packed (quartz) or with large voids (zeolites)
- Important class of compounds in geochemistry and industry (molecular sieves, catalysts)
- Zeolite unit cells can contain hundreds of atoms



# SiO<sub>2</sub> polymorphs and zeolites – Fitting training set

- DFT GGA-PBE calculations on  $\alpha$ -quartz, tridymite and Linde Type A
- Plane-wave cutoff 510 eV, k-spacing 0.178  $\text{\AA}^{-1}$
- Grimme D3 correction
  
- 206  $\alpha$ -quartz, 341 tridymite and 1184 Linde type A structures
- 90 Linde type A structures with up to three water molecules
- 1821 structures in total
  - Ab initio MD trajectories
  - Systematic distortions of cell parameters and bonds
  
- MLPs: GRACE-1L and GRACE-2L
- Cutoff 6.0  $\text{\AA}$  and 10.0  $\text{\AA}$ , energy weight 1.0, force weight 5.0



# SiO<sub>2</sub> polymorphs and zeolites – Fit quality

|                |                 | GRACE-1L, 6 Å | GRACE-1L, 10 Å | GRACE-2L   |
|----------------|-----------------|---------------|----------------|------------|
| Training set   | Energies, RMSE  | 0.9           | 1.5            | 1.0        |
|                | Energies, MAE   | 0.7           | 1.1            | 0.8        |
|                | Forces, RMSE    | 19.2          | 18.4           | 12.0       |
|                | Forces, MAE     | 12.5          | 12.3           | 8.1        |
| Validation set | Energies, RMSE  | 0.5           | 1.5            | 0.6        |
|                | Energies, MAE   | 0.3           | 0.5            | 0.3        |
|                | Forces, RMSE    | 39.2          | 33.9           | 27.1       |
|                | Forces, MAE     | 16.7          | 14.7           | 10.4       |
| Run time       | 1000 iterations | 12 h 51 min   | 30 h 41 min    | 24 h 3 min |

Energies in meV/atom, forces in meV/Å, run times on Nvidia Geforce RTX 3060

# SiO<sub>2</sub> Polymorphs and Zeolites – MLP Transferability

- LAMMPS minimization, GRACE-1L, cutoff 6 Å

|                          | a(exp.)  | b(exp.)  | c(exp.)  | dev. a [%] | dev. b [%] | dev. c [%] |
|--------------------------|----------|----------|----------|------------|------------|------------|
| α-quartz                 | 4.91     | 4.91     | 5.4      | 1.1        | 0.8        | 1.0        |
| β-quartz                 | 5        | 5        | 5.46     | 1.3        | 1.3        | 2.5        |
| β-cristobalite (high)    | 7.16     | 7.16     | 7.16     | 173.0      | 173.0      | 173.0      |
| α-cristobalite (low)     | 4.9709   | 4.9709   | 6.9278   | 1.5        | 1.5        | 1.4        |
| Faujasite                | 24.26    | 24.26    | 24.26    | 1.4        | 1.4        | 1.4        |
| ZSM-5                    | 20.02    | 19.9     | 13.38    | 1.6        | 0.6        | 0.7        |
| Mordenite                | 18.09    | 20.52    | 7.52     | 1.6        | 0.5        | 0.7        |
| Zeolite Rho              | 14.88    | 14.88    | 14.88    | 1.0        | 1.0        | 1.0        |
| Sodalite                 | 8.83     | 8.83     | 8.83     | 2.3        | 2.3        | 2.3        |
| Tridymite                | 18.524   | 5.003    | 23.81    | 1.3        | 1.1        | 1.3        |
| Coesite                  | 7.136    | 12.369   | 7.174    | 0.8        | 1.0        | 0.9        |
| Chabazite                | 13.675   | 13.675   | 14.767   | 0.7        | 0.6        | 0.8        |
| Linde Type A             | 11.919   | 11.919   | 11.919   | 0.7        | 0.7        | 0.7        |
| Linde Type A (Si/Al = 3) | (11.919) | (11.919) | (11.919) | 2.5        | 2.1        | 2.0        |
| ZSM-5 (Si/Al = 95)       | (20.02)  | (19.9)   | (13.38)  | 1.6        | 0.3        | 0.3        |
| Linde Type A (Si/Al = 5) | (11.919) | (11.919) | (11.919) | 1.6        | 2.3        | 1.1        |

# SiO<sub>2</sub> Polymorphs and Zeolites – MLP Transferability

- LAMMPS minimization, GRACE-1L, cutoff 10 Å

|                          | a(exp.)  | b(exp.)  | c(exp.)  | dev. a [%] | dev. b [%] | dev. c [%] |
|--------------------------|----------|----------|----------|------------|------------|------------|
| α-quartz                 | 4.91     | 4.91     | 5.4      | 1.0        | 0.8        | 1.1        |
| β-quartz                 | 5        | 5        | 5.46     | 1.0        | 0.8        | 3.2        |
| β-cristobalite (high)    | 7.16     | 7.16     | 7.16     | 126.5      | 126.5      | 126.5      |
| α-cristobalite (low)     | 4.9709   | 4.9709   | 6.9278   | 1.4        | 1.4        | 1.4        |
| Faujasite                | 24.26    | 24.26    | 24.26    | 1.2        | 1.2        | 1.2        |
| ZSM-5                    | 20.02    | 19.9     | 13.38    | 1.4        | 0.2        | 0.3        |
| Mordenite                | 18.09    | 20.52    | 7.52     | 1.3        | 0.2        | 0.7        |
| Zeolite Rho              | 14.88    | 14.88    | 14.88    | 0.8        | 0.8        | 0.8        |
| Sodalite                 | 8.83     | 8.83     | 8.83     | 2.2        | 2.2        | 2.2        |
| Tridymite                | 18.524   | 5.003    | 23.81    | 1.3        | 1.3        | 1.4        |
| Coesite                  | 7.136    | 12.369   | 7.174    | 1.1        | 1.0        | 0.9        |
| Chabazite                | 13.675   | 13.675   | 14.767   | 0.4        | 0.4        | 0.5        |
| Linde Type A             | 11.919   | 11.919   | 11.919   | 0.5        | 0.5        | 0.5        |
| Linde Type A (Si/Al = 3) | (11.919) | (11.919) | (11.919) | 2.5        | 2.1        | 1.8        |
| ZSM-5 (Si/Al = 95)       | (20.02)  | (19.9)   | (13.38)  | 1.4        | 0.1        | 0.1        |
| Linde Type A (Si/Al = 5) | (11.919) | (11.919) | (11.919) | 1.5        | 2.1        | 0.7        |

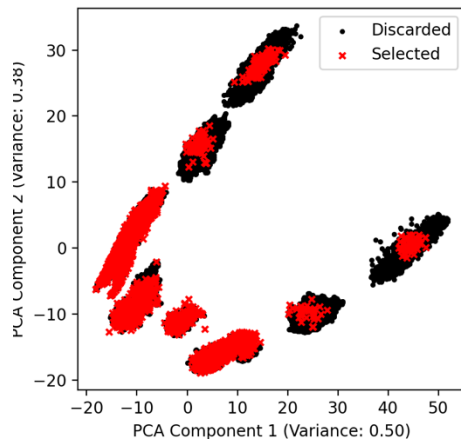
# SiO<sub>2</sub> Polymorphs and Zeolites – MLP Transferability

- LAMMPS minimization, GRACE-2L, cutoff 6 Å

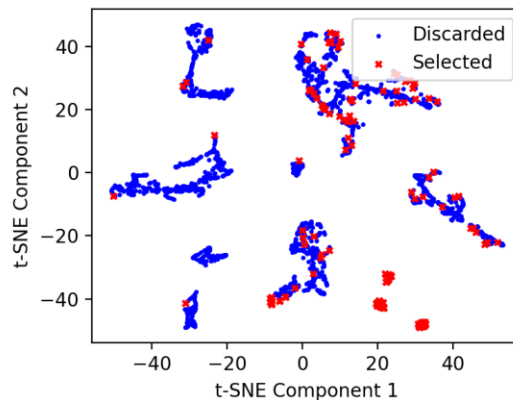
|                          | a(exp.)  | b(exp.)  | c(exp.)  | dev. a [%] | dev. b [%] | dev. c [%] |
|--------------------------|----------|----------|----------|------------|------------|------------|
| α-quartz                 | 4.91     | 4.91     | 5.4      | 1.0        | 0.8        | 1.1        |
| β-quartz                 | 5        | 5        | 5.46     | 1.2        | 0.9        | 2.8        |
| β-cristobalite (high)    | 7.16     | 7.16     | 7.16     | -1.2       | -1.2       | -1.2       |
| α-cristobalite (low)     | 4.9709   | 4.9709   | 6.9278   | 1.4        | 1.4        | 1.3        |
| Faujasite                | 24.26    | 24.26    | 24.26    | 1.2        | 1.2        | 1.2        |
| ZSM-5                    | 20.02    | 19.9     | 13.38    | 1.5        | 0.4        | 0.4        |
| Mordenite                | 18.09    | 20.52    | 7.52     | 1.6        | 0.5        | 0.7        |
| Zeolite Rho              | 14.88    | 14.88    | 14.88    | 0.8        | 0.8        | 0.8        |
| Sodalite                 | 8.83     | 8.83     | 8.83     | 2.2        | 2.2        | 2.2        |
| Tridymite                | 18.524   | 5.003    | 23.81    | 1.3        | 1.2        | 1.3        |
| Coesite                  | 7.136    | 12.369   | 7.174    | 1.2        | 1.0        | 1.0        |
| Chabazite                | 13.675   | 13.675   | 14.767   | 0.5        | 0.5        | 0.6        |
| Linde Type A             | 11.919   | 11.919   | 11.919   | 0.6        | 0.6        | 0.6        |
| Linde Type A (Si/Al = 3) | (11.919) | (11.919) | (11.919) | 2.3        | 2.1        | 1.8        |
| ZSM-5 (Si/Al = 95)       | (20.02)  | (19.9)   | (13.38)  | 1.3        | 0.2        | 0.1        |
| Linde Type A (Si/Al = 5) | (11.919) | (11.919) | (11.919) | 1.4        | 2.0        | 0.7        |

# SiO<sub>2</sub> Polymorphs and Zeolites – Similarity Analysis

- Structures in a fitting data set can be compared using a similarity analysis
- Uses Smooth Overlap of Atomic Positions (SOAP)<sup>a</sup> descriptor
- Reduce training set size to run first principles calculations only on diverse structures (e. g., from a dynamics run with a foundation model)
- Fitting dataset reduced to 128 structures



Principal Components Analysis



t-distributed Stochastic Neighbor Embedding

<sup>a</sup> Sandip De, Albert P. Bartók, Gábor Csányi, and Michele Ceriotti: Comparing molecules and solids across structural and alchemical space. *Phys. Chem. Chem. Phys.*, **18(20)** (2016), 13754–13769

# SiO<sub>2</sub> polymorphs and zeolites – Similarity Analysis

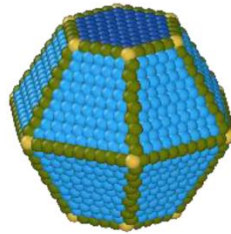
|                |                 | GRACE-1L, 6 Å | GRACE-1L, 10 Å | GRACE-2L,<br>1821 structures | GRACE-2L,<br>128 structures |
|----------------|-----------------|---------------|----------------|------------------------------|-----------------------------|
| Training set   | Energies, RMSE  | 0.9           | 1.5            | 1.0                          | 11.1                        |
|                | Energies, MAE   | 0.7           | 1.1            | 0.8                          | 8.8                         |
|                | Forces, RMSE    | 19.2          | 18.4           | 12.0                         | 170.6                       |
|                | Forces, MAE     | 12.5          | 12.3           | 8.1                          | 79.0                        |
| Validation set | Energies, RMSE  | 0.5           | 1.5            | 0.6                          | 4.7                         |
|                | Energies, MAE   | 0.3           | 0.5            | 0.3                          | 3.8                         |
|                | Forces, RMSE    | 39.2          | 33.9           | 27.1                         | 102.5                       |
|                | Forces, MAE     | 16.7          | 14.7           | 10.4                         | 68.6                        |
| Run time       | 1000 iterations | 12 h 51 min   | 30 h 41 min    | 24 h 3 min                   | 6 h 30 min                  |

Energies in meV/atom, forces in meV/Å, run times on Nvidia Geforce RTX 3060

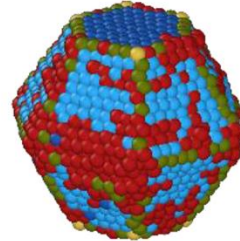
# SiO<sub>2</sub> Polymorphs and Zeolites – Similarity Analysis

|                          | GRACE-2L, 1821 structures |            |            | GRACE-2L, 128 structures |            |            |
|--------------------------|---------------------------|------------|------------|--------------------------|------------|------------|
|                          | dev. a [%]                | dev. b [%] | dev. c [%] | dev. a [%]               | dev. b [%] | dev. c [%] |
| α-quartz                 | 1.0                       | 0.8        | 1.1        | 0.7                      | 0.5        | 1.1        |
| β-quartz                 | 1.2                       | 0.9        | 2.8        | 3.2                      | 3.1        | -0.4       |
| β-cristobalite (high)    | -1.2                      | -1.2       | -1.2       | 8.6                      | 8.6        | 8.6        |
| α-cristobalite (low)     | 1.4                       | 1.4        | 1.3        | 1.8                      | 1.8        | 1.5        |
| Faujasite                | 1.2                       | 1.2        | 1.2        | 0.4                      | 0.4        | 0.4        |
| ZSM-5                    | 1.5                       | 0.4        | 0.4        | -0.1                     | -1.9       | -0.9       |
| Mordenite                | 1.6                       | 0.5        | 0.7        | 0.8                      | 0.0        | 0.0        |
| Zeolite Rho              | 0.8                       | 0.8        | 0.8        | -0.1                     | -0.1       | -0.1       |
| Sodalite                 | 2.2                       | 2.2        | 2.2        | 1.3                      | 1.3        | 1.3        |
| Tridymite                | 1.3                       | 1.2        | 1.3        | 1.1                      | 1.1        | 1.5        |
| Coesite                  | 1.2                       | 1.0        | 1.0        | 1.9                      | -53.6      | -23.8      |
| Chabazite                | 0.5                       | 0.5        | 0.6        | -0.3                     | -0.3       | -0.1       |
| Linde Type A             | 0.6                       | 0.6        | 0.6        | -0.2                     | -0.2       | -0.2       |
| Linde Type A (Si/Al = 3) | 2.3                       | 2.1        | 1.8        | 0.0                      | -0.2       | -0.2       |
| ZSM-5 (Si/Al = 95)       | 1.3                       | 0.2        | 0.1        | 0.6                      | -0.4       | -0.8       |
| Linde Type A (Si/Al = 5) | 1.4                       | 2.0        | 0.7        | -0.6                     | -0.9       | -1.7       |

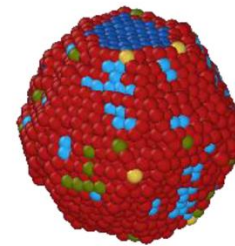
# Co Nanoclusters



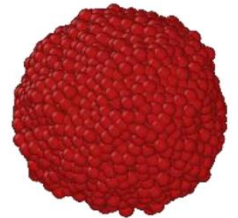
0 K



900 K

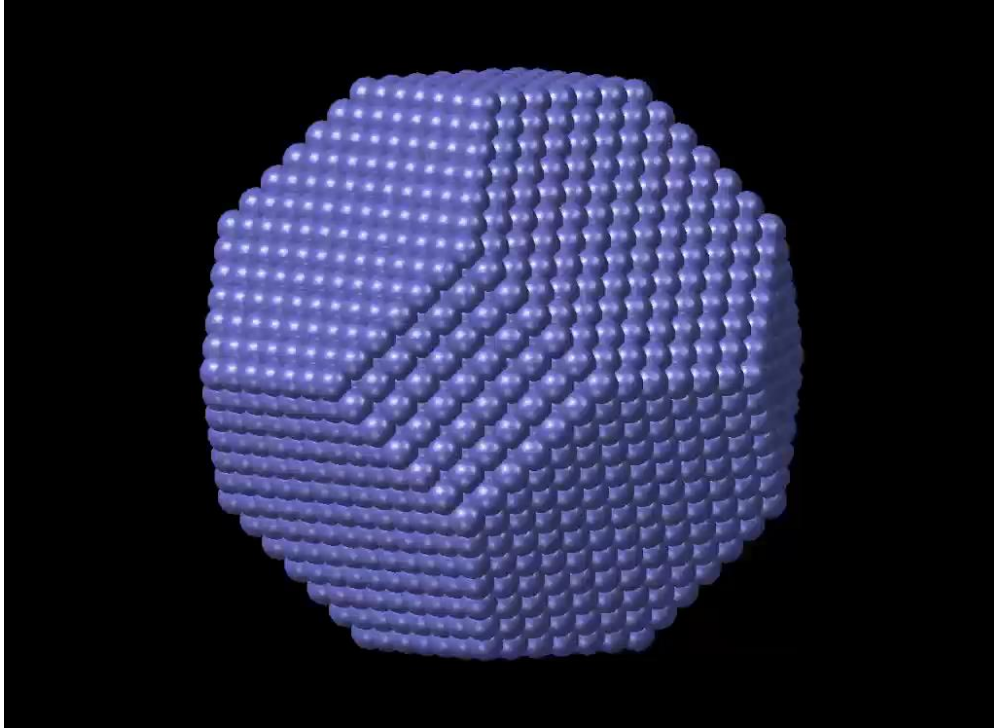


1150 K



1480 K

# Dynamics of Co Nanoparticles: A Machine Learning Approach<sup>1</sup>

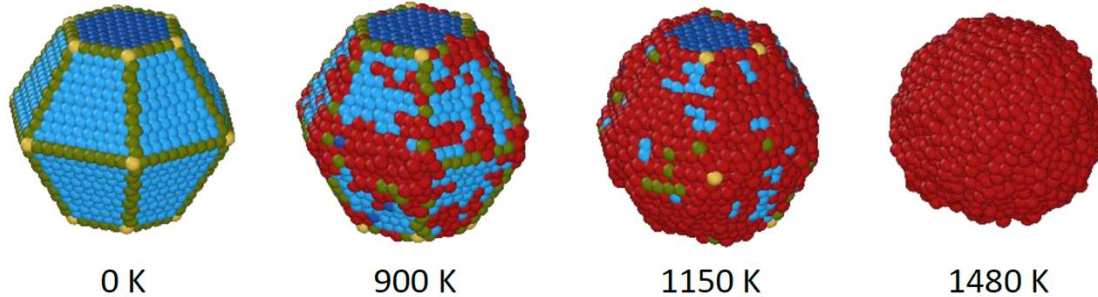


Molecular dynamics simulation of a truncated octahedral fcc Co nanoparticle using a machine-learning potential [1].

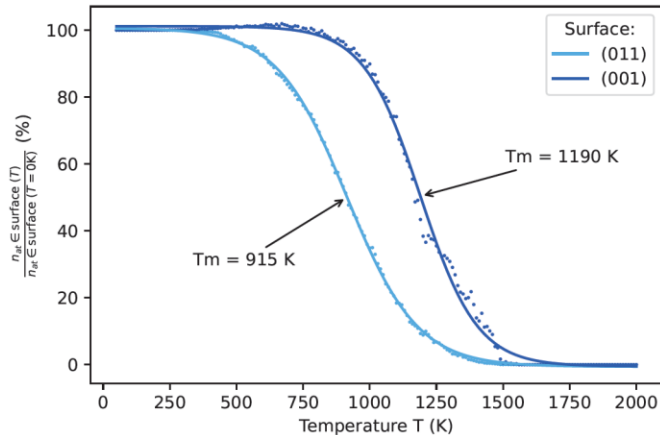
Heating from 1 K to 2000 K in 30 ps

[1] M. Bideault, J. Creuze, R. Asahi, and E. Wimmer, Polyvalent machine-learned potential for cobalt: From bulk to nanoparticles, *Phys. Rev. Materials* **8**, 123803 (2024)

# Dynamics of Co Nanoparticles: A Machine Learning Approach<sup>1</sup>



Classification of atoms using machine learning with a bispectrum descriptor



- The (011) facets of an hcp-type nanoparticle melt at 915 K
- The (001) facets are more stable, melting at 1190 K
- The entire nanoparticle melts at 1480 K
- The computed melting point of bulk Co is  $1695 \pm 15 \text{ K}$ ; experiments: 1768 K and 1770 K

[1] M. Bideault, J. Creuze, R. Asahi, and E. Wimmer, Polyvalent machine-learned potential for cobalt: From bulk to nanoparticles, Phys. Rev. Materials **8**, 123803 (2024)

# MedeA MLP/MLPG

## VASP accuracy with LAMMPS speed at your fingertips all within MedeA

- Machine-Learned-Potentials (MLPs) offer a combination of extended length and time scales with unprecedented ease in generation and high fidelity with respect to DFT to describe so far inaccessible physical phenomena.
- The *MedeA* MLP Generator (MLPG) offers a fully integrated workflow from training-set generation (using *MedeA* HT) and MLP generation to MLP application using *MedeA* LAMMPS.
- Foundational GRACE potentials are ready to use with *MedeA* LAMMPS.

# Question and Answer Session



***Dr. Volker Eyert***

*Materials Design*



***Dr. Jörg-Rüdiger Hill***

*Materials Design*

# Questions about Materials Design Webinars

***Katherine Hollingsworth***

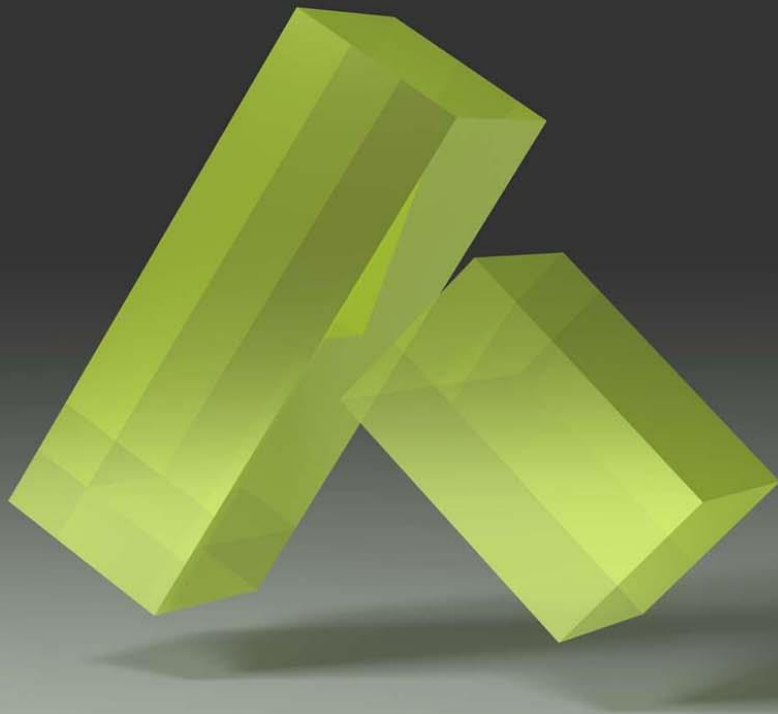
*khollingsworth@materialsdesign.com*



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# MedeA

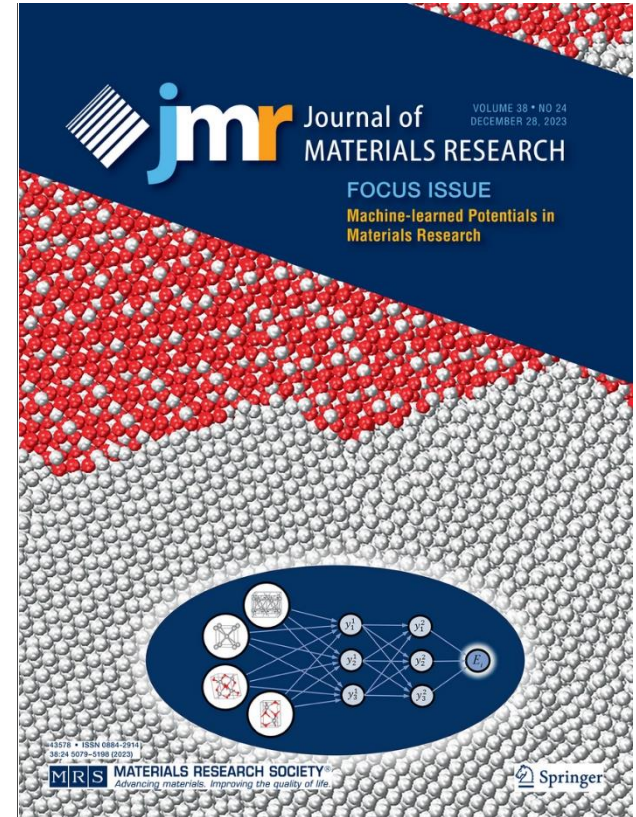
*Innovation by Simulation*



# Additional Material

# JMR Focus Issue on MLPs

- [J. Mater. Res. 38\(24\), 2023](#)
- Guest editors: Volker Eyert, Jonathan Wormald, William A. Curtin, Erich Wimmer
- Introductory article by guest editors
- Nine additional publications
  - Combination of methodology and applications
  - Two invited feature articles: Ralf Drautz *et al.*, Aidan Thompson, Mitchell Wood *et al.*
  - Seven invited articles: Gus Hart *et al.*, Ryoji Asahi *et al.*, Alexander Shapeev *et al.*, Michele Ceriotti, William Curtin *et al.*, Jörg-Rüdiger Hill and Wolfgang Mannstadt



# Introductory Paper

- Historical outline from classical forcefields to machine-learned potentials
- Key features of MLPs
- Approaches to generate MLPs
- MLFF, active learning,  $\Delta$ -learning
- Basic concepts (descriptors, regressors)
- Applications of MLPs (literature survey)
- Overview of the Focus Issue
- Perspectives



## MACHINE-LEARNED POTENTIALS IN MATERIALS RESEARCH

## Machine-learned interatomic potentials: Recent developments and prospective applications

Volker Eyert<sup>1,2,a</sup>, Jonathan Wormald<sup>3</sup>, William A. Curtin<sup>4</sup>, Erich Wimmer<sup>1,2</sup><sup>1</sup>Materials Design, Inc., San Diego, CA, USA<sup>2</sup>Materials Design SARL, Montrouge, France<sup>3</sup>Naval Nuclear Laboratory, West Mifflin, PA, USA<sup>4</sup>Ecole Polytechnique Fédérale de Lausanne, Evryville, Switzerland<sup>a</sup>Address all correspondence to this author. e-mail: veyert@materialsdesign.com

Volker Eyert, Jonathan Wormald, William A. Curtin, and Erich Wimmer were guest editors of this journal during the review and decision stage. For the JMR policy on review and publication of manuscripts authored by editors, please refer to <http://www.nmr.org/editor-manuscripts/>.

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High-throughput generation of large and consistent *ab initio* data combined with advanced machine-learning techniques are enabling the creation of interatomic potentials of near *ab initio* quality. This capability has the potential of dramatically impacting materials research: (i) while classical interatomic potentials have become indispensable in atomistic simulations, such potentials are typically restricted to certain classes of materials. Machine-learned potentials (MLPs) are applicable to all classes of materials individually and, importantly, to any combinations of them; (ii) MLPs are by design reactive force fields. This Focus Issue provides an overview of the state of the art of MLPs by presenting a range of impressive applications including metallurgy, photovoltaics, proton transport, nanoparticles for catalysis, ionic conductors for solid state batteries, and crystal structure predictions. These investigations provide insight into the current challenges, and they present pathways for their solutions, thus setting the stage for exciting perspectives in computational materials research.

### Introduction

To appreciate the distinct features and innovative character of interatomic potentials obtained with machine learning techniques, let us briefly highlight the key aspects of classical potentials or force fields. In both machine learning and classical approaches, the motivation is the same, namely atomistic simulations of large systems, sampling the configurational space and dynamic processes in a statistically meaningful way. In the absence of any better way, such interatomic potentials were originally fitted to empirical data such as vibrations of molecules and the structure of crystalline solids [1, 2], elastic coefficients, thermal expansion coefficients, and thermodynamic properties of fluids. This led to ground-breaking work by pioneers such as Anandarajaraman [3]. A major driver in the development of force fields in the 1980's was the desire to perform molecular simulations of DNA and proteins and their interaction with drug molecules. This led to the development of force fields such as

ECEPP by the group of Harald Scheraga at Cornell University, the CHARMM force field in the group of Martin Karplus at Harvard, the AMBER forcefield by the group of Peter Kollman at the University of California in San Francisco, and the OPLS force field from the group of Jorgensen at Yale University. In this context, first versions of the consistent force field (CFF) were developed by Lifson, Hagler and Duanke [4]. An interesting approach was pursued in the group of Norman Allinger by including electronic aspects in a force field called MMP2 [5].

These classical force fields are based on a deep chemical understanding of the bonding and intermolecular interactions in molecular and bio-molecular systems. The various parameters were obtained largely by fitting to experimental data such as known interatomic distances and vibrational frequencies. A characteristic feature of these force fields is the atom-typing, i.e., the assignment of specific force field parameters based on a topological analysis of the environment of each atom. To a

# Datasheets, Tutorials, Documentation

M

## MedeA MLP

Efficient and Flexible Machine Learning Potential Support

**At-a-Glance**

MedeA<sup>®1</sup> MLP (Machine Learning Potential) provides full MedeA support for LAMMPS based machine learning potential simulations, including the simulation of mechanical, vibrational, and transport properties combined with comprehensive MedeA based analysis of simulation results.

MedeA MLP includes a library of published machine learning potentials derived from the machine learning Analysis Potential (SNAP)<sup>2</sup> Spectral Neighbor Analysis Potential (SNAP)<sup>2</sup> formalism supported by LAMMPS.

MedeA LAMMPS based simulations using MedeA MLP typically show excellent agreement with first-principles methods for systems that are well represented by the training set employed in creating the machine learning potential.

**Key Benefits**

**Productivity**

- Extends *ab initio* simulation results to larger length and time scales through substantially reduced energy and force calculation times
- Efficient use of published machine learning potentials
- Automates the handling of files and data for efficient simulation

**Access**

- Supports the SNAP machine learning potential form
- Allows access to all MedeA LAMMPS simulation properties with machine learning potential accuracy
- Can be employed with the Machine Learning Potential Generator (MedeA MLPG) to access newly derived machine learning potentials
- Handles diverse atomic geometries including making and breaking of bonds

Machine learning methods allow rich first-principles datasets to be mined and employed in interpolation and inference. Such techniques are having a dramatic effect in many areas of science. In materials science, they allow researchers to obtain the accuracy and freedom from bias of *ab initio* methods at reasonable computational cost for substantial simulation times and system sizes.

*'All science depends on past work. Machine Learning depends more than other science on previous work: it needs examples.'*

Michael Levitt, Nobel Laureate.

**Key Features**

- Library of published machine learning potentials
- Full support for the SNAP description
- Enables LAMMPS MLP simulations in the MedeA Environment

**Required Modules**

MedeA Environment  
MedeA LAMMPS

**Related Modules**

MedeA MT  
MedeA Phonon  
MedeA Diffusion  
MedeA Surface Tension  
MedeA Thermal Conductivity

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Learn more about Machine Learning by watching our recorded Machine Learning-Quantum% Emistry-Catalysts

Deng, R. Tran, H. Tang, J. H. Chu, S. P. Ong, *in situ* for molybdenum by machine learning  
Hu, C. Chen, Z. Deng, J. Luo, S. P. Ong  
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## MedeA MLPG

Efficient Flexible Machine Learning Potential Generator

**At-a-Glance**

The MedeA<sup>®1</sup> MLPG (Machine Learning Potential Generator) enables users to create their own machine learning potentials (or force-fields) from training-set data previously generated by quantum mechanical calculations. The resulting potentials allow users to perform simulations of systems substantially larger in size and for much larger simulation times than can be typically accessed using quantum mechanical methods while at the same time reflecting the high accuracy and validity of the latter.

In addition to managing selection of training and validation data, the MedeA MLPG allows you to generate machine learning potentials, using the Spectral Neighbor Analysis Potential (SNAP)<sup>2</sup> formalisms. The potentials created are ready for subsequent use with MedeA MLP. Combined with the MedeA Flowchart interface as well as VASP<sup>3</sup> and LAMMPS, the MedeA MLPG thus provides efficient access to machine learning based simulation techniques.

**Key Benefits**

**Productivity**

- Automates the creation of machine learning potentials using the SNAP formalism
- Extends *ab initio* precision to larger length and time scales
- Manages training set data
- Full Ziegler-Biersack-Litmark (ZBL) potential support

**Accuracy**

- Yields machine learning descriptions based on the SNAP methods
- Provides access to all calculation details and information
- Provides machine learning potentials for use with all MedeA LAMMPS property calculation types

Machine learning potentials employ efficient descriptors of atomic environments combined with machine learning based correlative methods to describe the energetic behavior of atomic and molecular systems. The MedeA MLPG allows users to generate machine learning potentials by accurately reproducing supplied target first-principles data for a training set of structures.



**Figure 1:** The MedeA Machine Learning Potential Generator (MLPG) is integrated within the MedeA environment allowing straightforward use of first-principles information from VASP in the creation of MLPs.

The MedeA MLPG manages training-set data derived from first-principles calculations as the target to be reproduced by the MLP (machine learning potential). Configuration dependent energies, forces, and stresses can be considered in the fitting process. Using the SNAP approach the MedeA MLPG creates a machine learning potential by minimizing the deviations from the target energies, forces, and stresses calculated by quantum mechanical methods. While this process is guided by meaningful default parameters, the full flexibility of the underlying methods can be accessed by advanced settings. The MedeA MLPG has been developed as part of active research and development projects and is thoroughly validated.

**Technical Features**

- Selection of training and validation data
- Specification of terms for optimization
- Report and plot creation for analysis

**User Interface**

- Interactive selection and control of automated results analysis
- Efficient handling of optimization

**Supported Target Data**

Energies  
Forces  
Stress tensors

**Key Features**

Uses VASP derived DFT results  
Interactive selection and control of automated results analysis  
Efficient handling of optimization

**Required Modules**

MedeA Environment  
VASP  
LAMMPS

**Modules**

MedeA Phonon  
MedeA Diffusion  
MedeA Surface Tension  
MedeA Thermal Conductivity

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# Related *MedeA* Webinars

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**Ab Initio for Millions - the Power of Machine-learned Potentials:**

<https://www.materialsdesign.com/webinars/recorded/Ab-Initio-for-MLPG>

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***MedeA* Training: *MedeA* Machine Learning Potential Generator (MLPG):**

<https://www.materialsdesign.com/webinars/recorded/UGM-2021-Training-MLPG>

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**VASP, Machine Learning, and Multi-Scale Physics: Defining the State of the Art in Materials Modeling:**

<https://www.materialsdesign.com/webinars/recorded/MedeA-VASP-Machine-Learning>

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**Training: Generating and Applying Machine-Learned Potentials with *MedeA*:**

<https://www.materialsdesign.com/webinars/recorded/UGMtraining-Generating-and-Appling-Machine-Learned-Potentials-with-MedeA>

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**On-the-fly Machine Learning Forcefields with *MedeA* VASP:**

<https://www.materialsdesign.com/webinars/recorded/MedeA-Training-On-the-Fly-Machine-Learning-Forcefields-with-MedeA-VASP>

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# Related *MedeA* Tutorials

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## **An Introduction to *MedeA* MLP:**

Learn how to run LAMMPS simulations with Machine Learning Potential

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## **An Introduction to *MedeA* MLPG:**

Learn how to generate machine-learned potentials within *MedeA*

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## **Generate a Ti Neural Network Machine-Learned Potential:**

Learn how to generate a neural network potential using *MedeA* MLPG

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## **Applying Delta-Learning to TiO<sub>2</sub> Machine-Learned Potentials:**

Learn how to use  $\Delta$ -learning to upgrade a machine-learned potential for TiO<sub>2</sub> from a lower first-principles level to a higher one

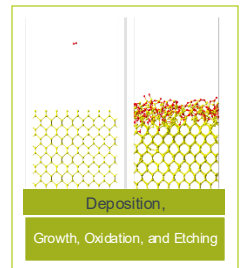
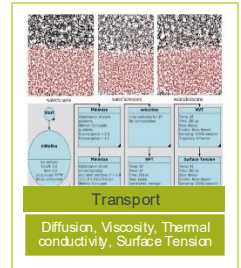
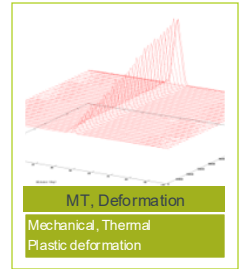
# Highlighted *MedeA* Modules

***MedeA* VASP:** Comprehensive access to the VASP Code via a graphical user interface (GUI) to set up, run and analyze multi-step VASP calculations

***MedeA* MLPG:** Fully integrated workflow from training-set generation (using *MedeA* HT) and MLP generation to MLP application using *MedeA* LAMMPS

***MedeA* HT:** Generation of large and consistent sets of computed data for input to machine learning procedures

***MedeA* LAMMPS:** Full access to the LAMMPS Code via a graphical user interface based on flowcharts to perform forcefield calculations using MLPs generated by *MedeA* MLPG



# MLPs with *MedeA* LAMMPS

**MedeA MT:** Elastic, mechanical and thermodynamic properties (also at finite temperature)

**MedeA Deformation:** Perform deformation beyond the elastic regime

**MedeA Thermal Conductivity:** Calculate lattice thermal conductivity with Green-Kubo or non-equilibrium MD Müller-Plathe

**MedeA Viscosity:** Calculate viscosity with Green-Kubo or non-equilibrium MD Müller-Plathe

**MedeA Surface Tension:** Calculate surface tension of fluid slabs

**MedeA Diffusion:** Automatically calculate diffusivity from mean square displacement

**MedeA Deposition:** Atomistic scale simulation to study deposition, growth, oxidation and etching

**MedeA Phonon:** Phonon spectra and thermodynamic functions (vibrational free energy, heat capacities)

